

Created by Mr. Lischwe

# Warmup 2 / (The 2<sup>nd</sup> perfect number)

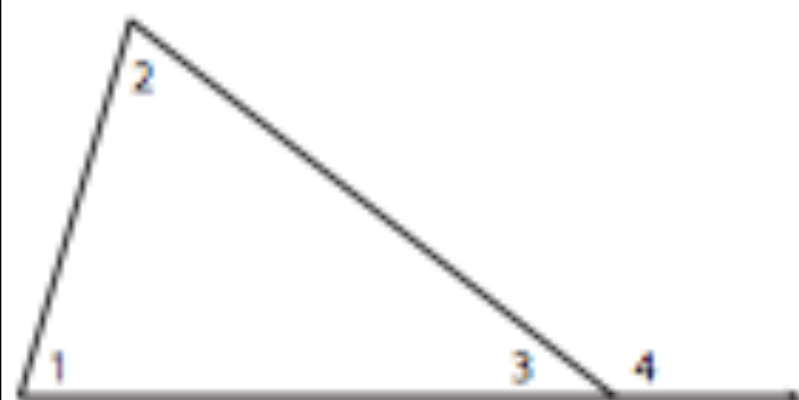
<b>45x</b>		<b>11+</b>		<b>2-</b>	
		<b>24x</b>		<b>30x</b>	<b>24x</b>
<b>240x</b>					
			<b>2÷</b>		<b>9x</b>
<b>11+</b>			<b>6</b>		
	<b>6</b>	<b>1-</b>		<b>4-</b>	

# Quiz Tuesday



## Triangle Properties

## Create a flow proof for the Exterior Angle Theorem



$$m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$$

Triangle Sum Theorem

$$m\angle 3 + m\angle 4 = 180^\circ$$

Definition of supplementary

$$m\angle 1 + m\angle 2 + m\angle 3 = m\angle 3 + m\angle 4$$

Substitution Property of Equality

$$m\angle 1 + m\angle 2 = m\angle 4$$

Subtraction Property of Equality

**11.** Find  $w$  to find the measure of the exterior angle.

$$w = 68 + 68$$

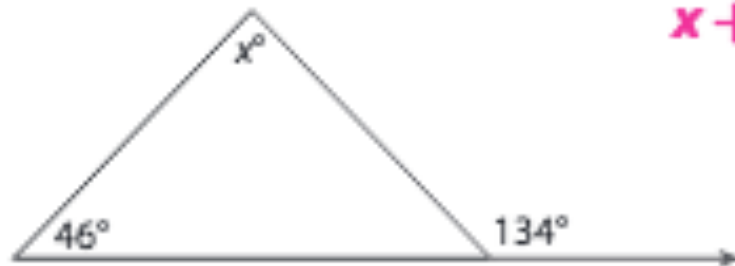
$$w = 136$$



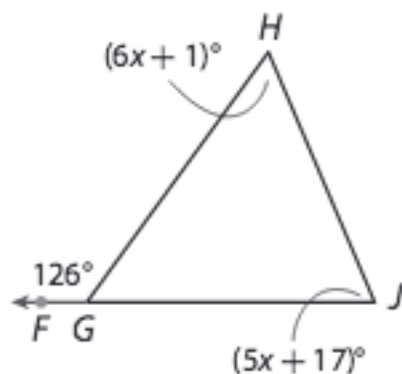
**12.** Find  $x$  to find the measure of the remote interior angle.

$$x + 46 = 134$$

$$x = 88$$



13. Find  $m\angle H$ .

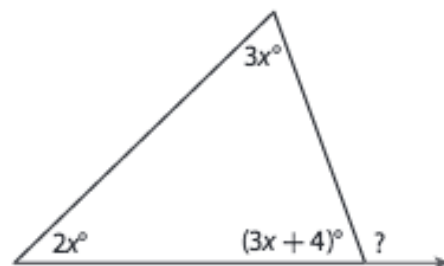


$$(6x - 1) + (5x + 17) = 126$$

$$x = 10$$

$$m\angle H = (6x - 1)^\circ = (6(10) - 1)^\circ = 59^\circ$$

14. Determine the measure of the indicated exterior angle in the diagram.



$$180 - (3x + 4) = 2x + 3x$$

$$22 = x$$

$$180 - (3(22) + 4) = 180 - (66 + 4) = 180 - 70 = 110$$

The measure of the indicated exterior angle is  $110^\circ$ .

15. Match each angle with its corresponding measure, given  $m\angle 1 = 130^\circ$  and  $m\angle 7 = 70^\circ$ . Indicate a match by writing the letter for the angle on the line in front of the corresponding angle measure.

A.  $m\angle 2$

    A      $50^\circ$

B.  $m\angle 3$

    B      $60^\circ$

C.  $m\angle 4$

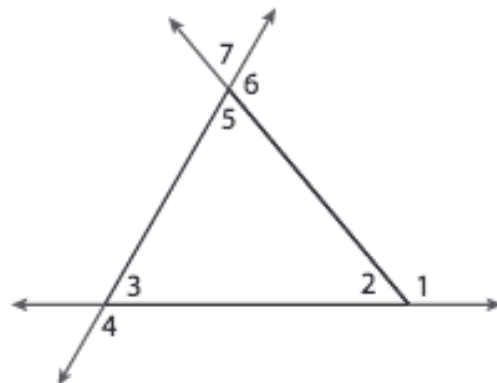
    D      $70^\circ$

D.  $m\angle 5$

    E      $110^\circ$

E.  $m\angle 6$

    C      $120^\circ$



A few minutes – compare/revise  
answers for the “angle chasing” sheet

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# Objective

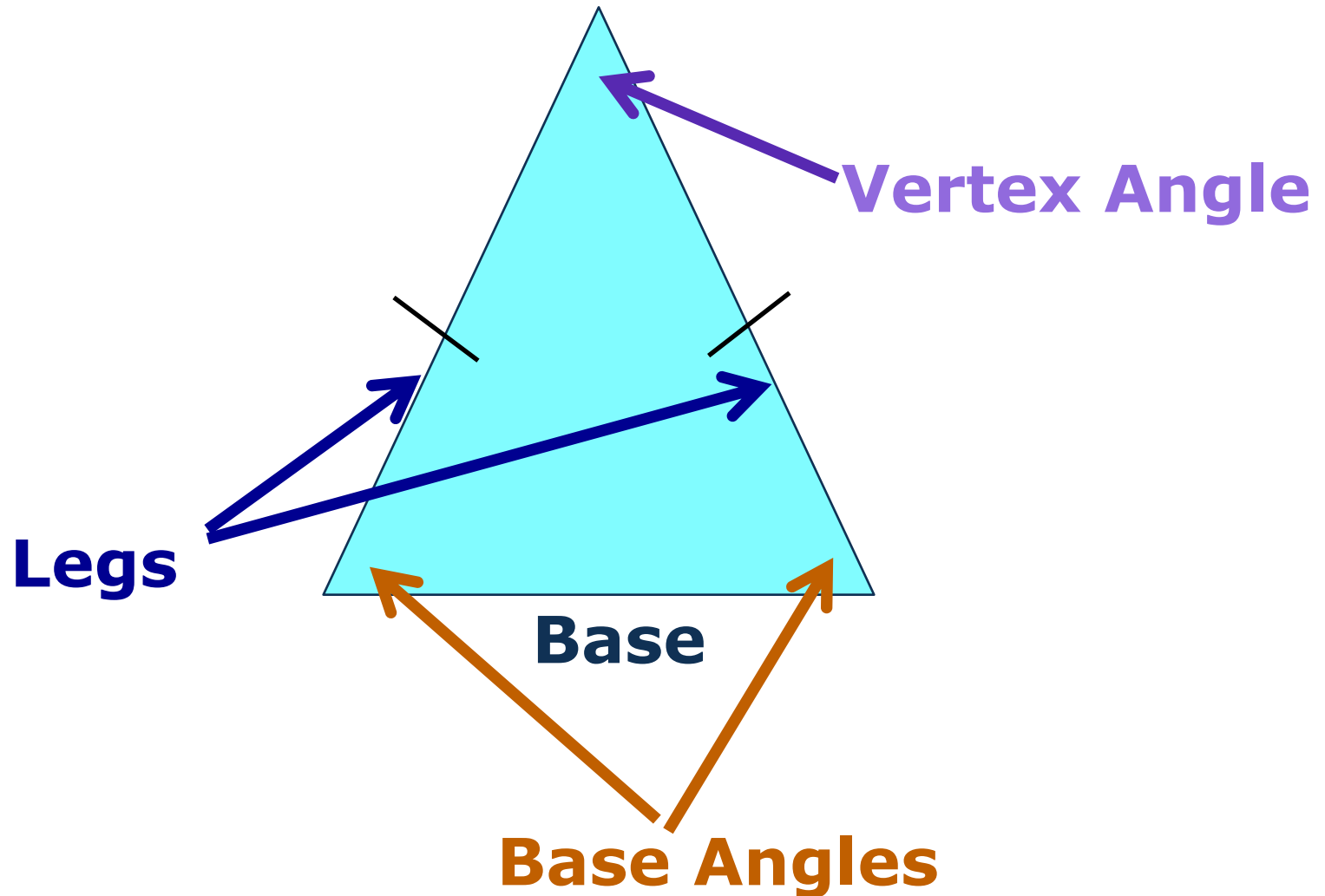


Explore Properties of Isosceles  
and Equilateral Triangles



# What is an Isosceles Triangle?

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# Activity

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- Draw an isosceles triangle using a ruler.
  - MEASURE THE SIDES!
- Measure the base angles using a protractor.
- Repeat this activity one more time.

What do you notice???

# Isosceles Triangle Theorem

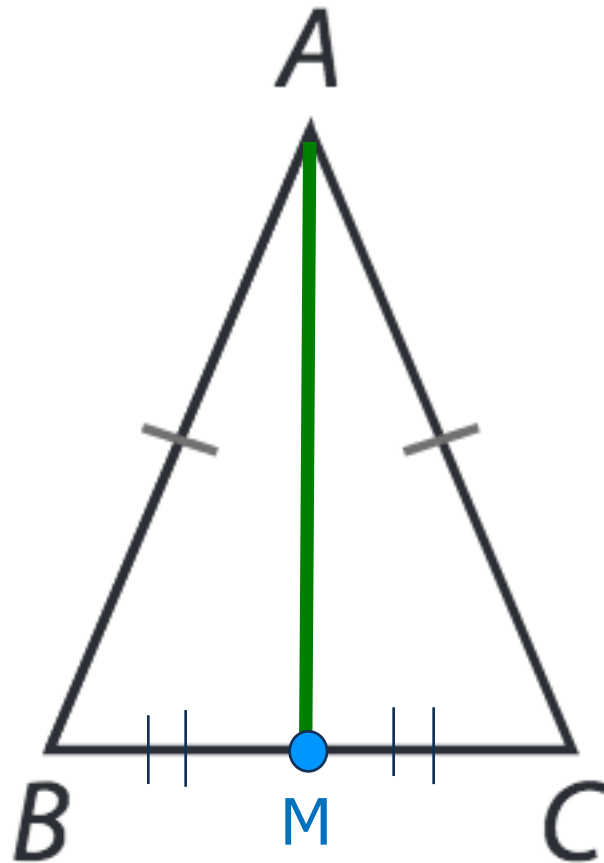
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pg. 1098

- If two sides of a triangle are congruent, then the two angles opposite the sides are congruent.
- in other words: “The Base Angles of an isosceles triangle are congruent”

Let's Prove this!

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# What is the converse of a theorem?

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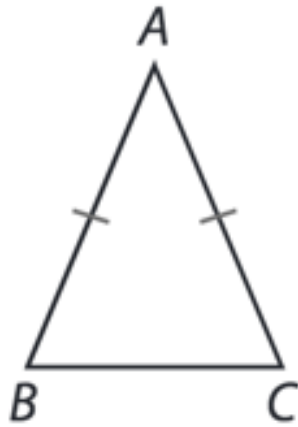
- A statement formed by interchanging what is given in a theorem and what is to be proved



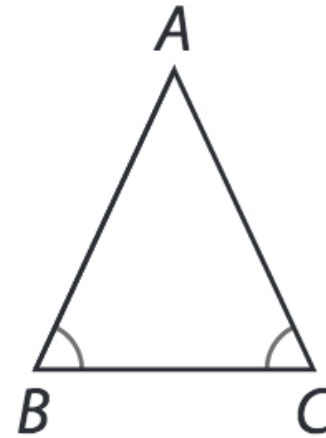
# Isosceles Triangle Theorem

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□ If

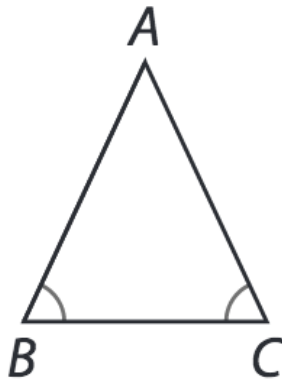


then



## Converse of the Isosceles Triangle Theorem

□ If



then



# Activity #2

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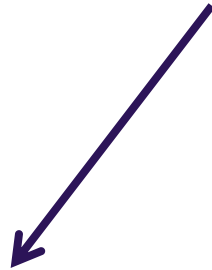
- Draw an equilateral triangle using a ruler.
  - MEASURE THE SIDES!
- Measure the angles using a protractor.
- Repeat this activity one more time.

What do you notice???

# Equilateral Triangle Theorem

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If a triangle is equilateral,  
then it is equiangular.

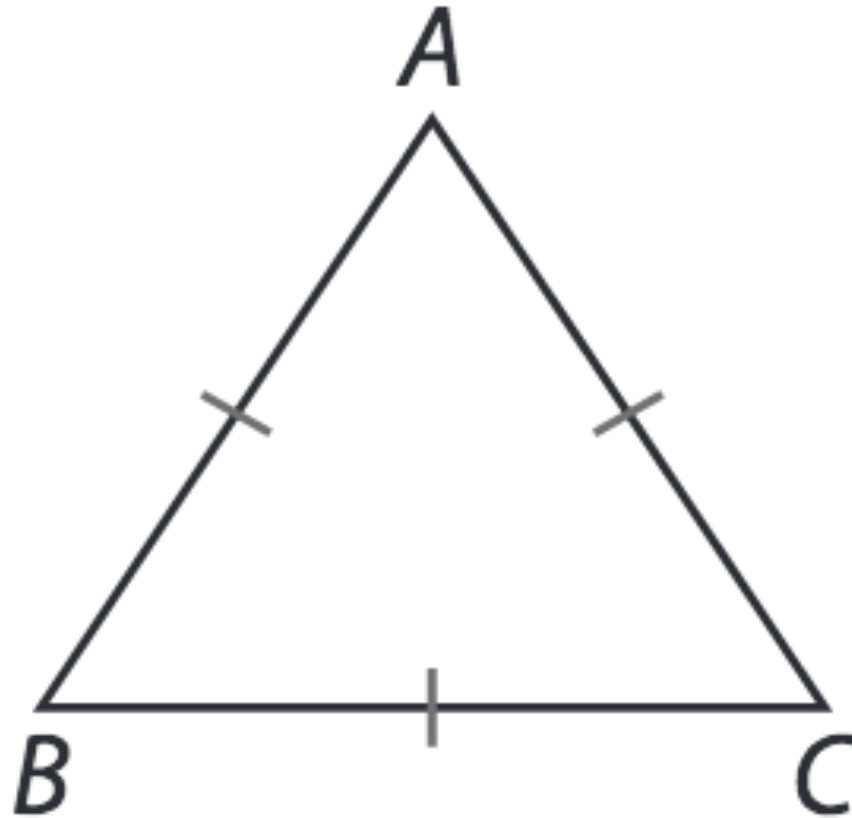


all angles have  
equal measures



Let's Prove this!

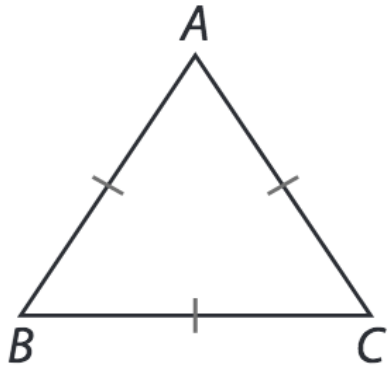
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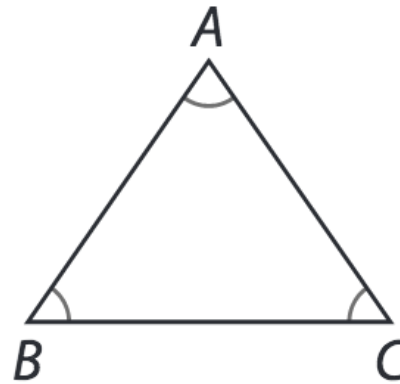
# Equilateral Triangle Theorem

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□ If

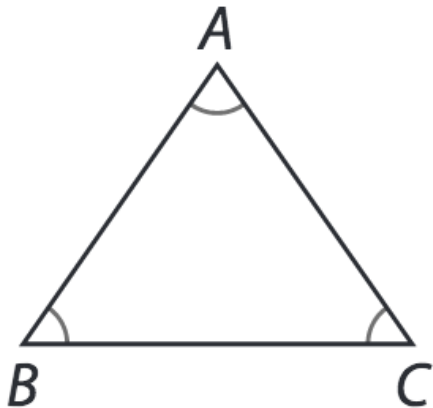


then

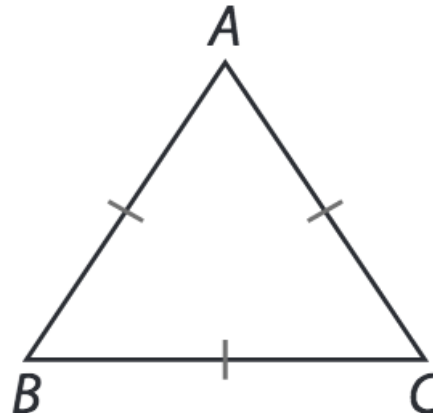


## Converse of the Equilateral Triangle Theorem

□ If

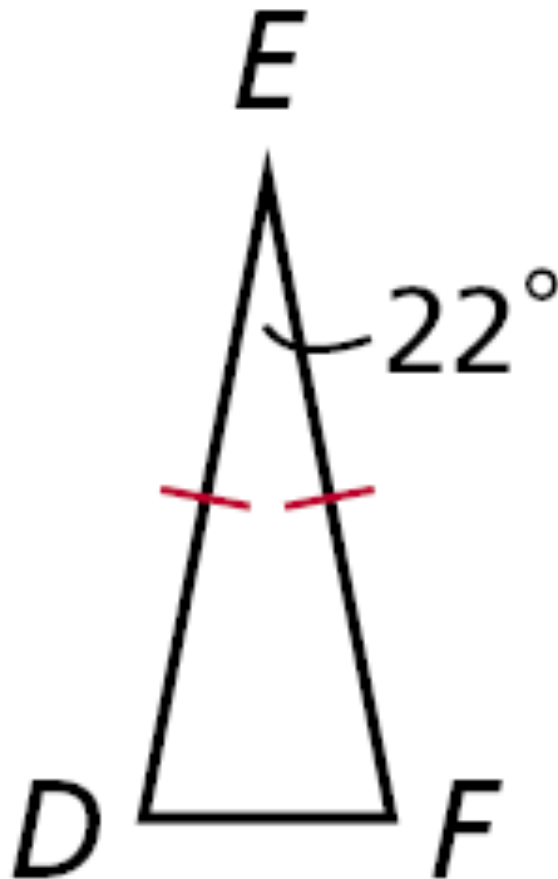


then



Find  $m\angle F$ .

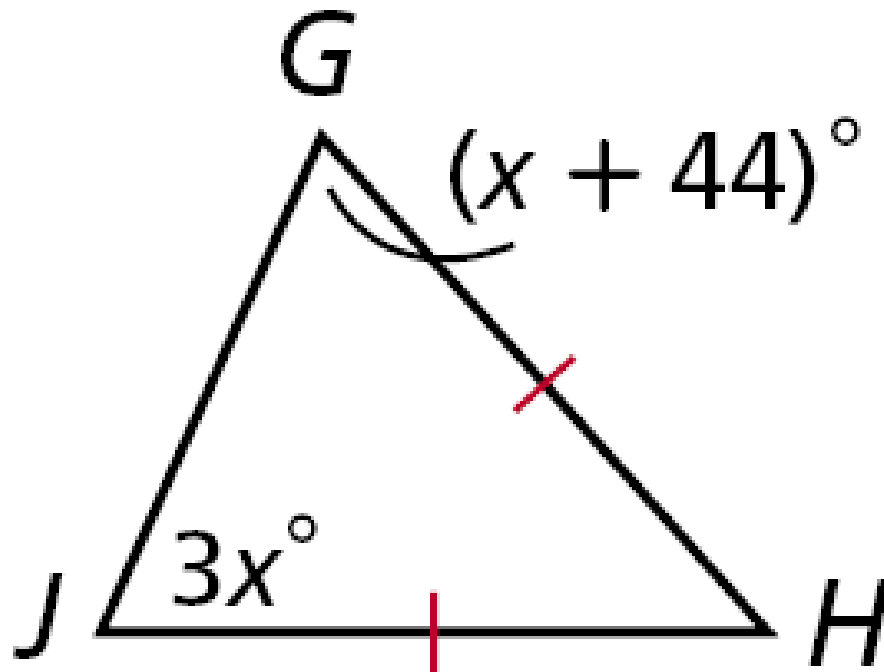
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$79^\circ$

# Find $m\angle G$ .

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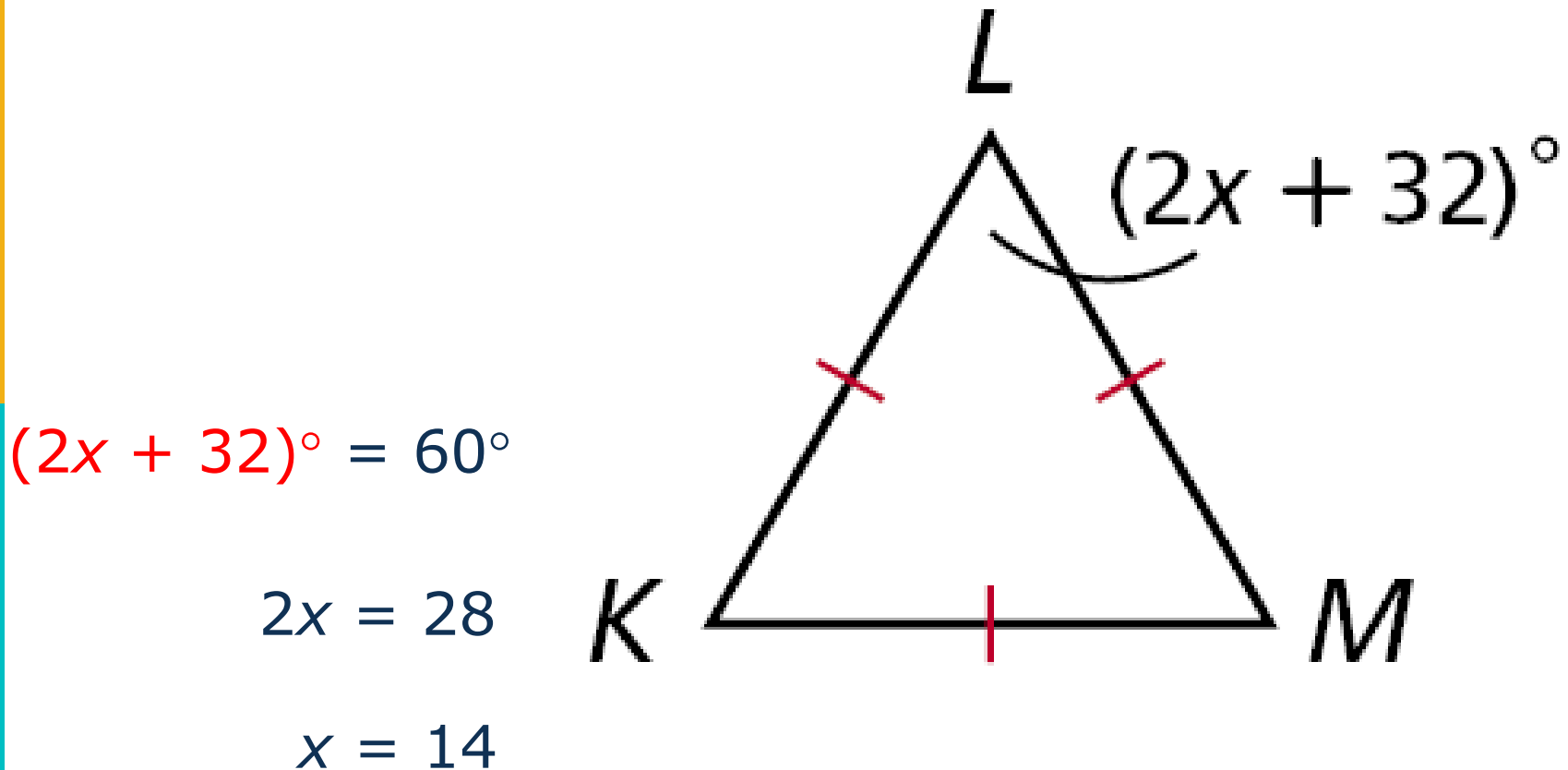
$$(x + 44)^\circ = 3x^\circ$$

$$x = 22^\circ$$

$$\text{Thus } m\angle G = 22^\circ + 44^\circ = 66^\circ .$$

# Find the value of $x$ .

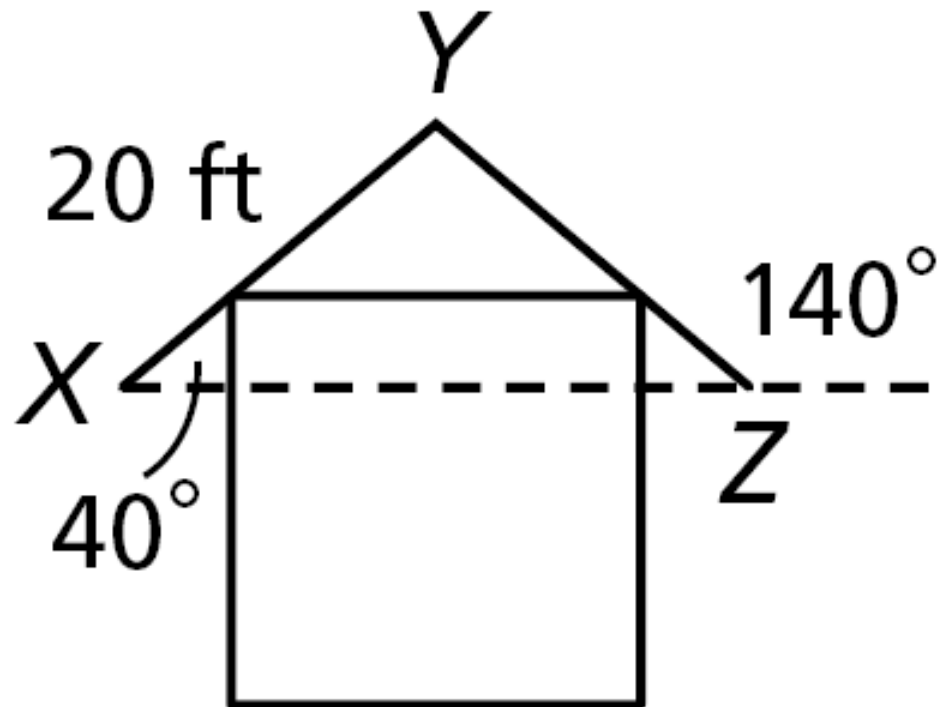
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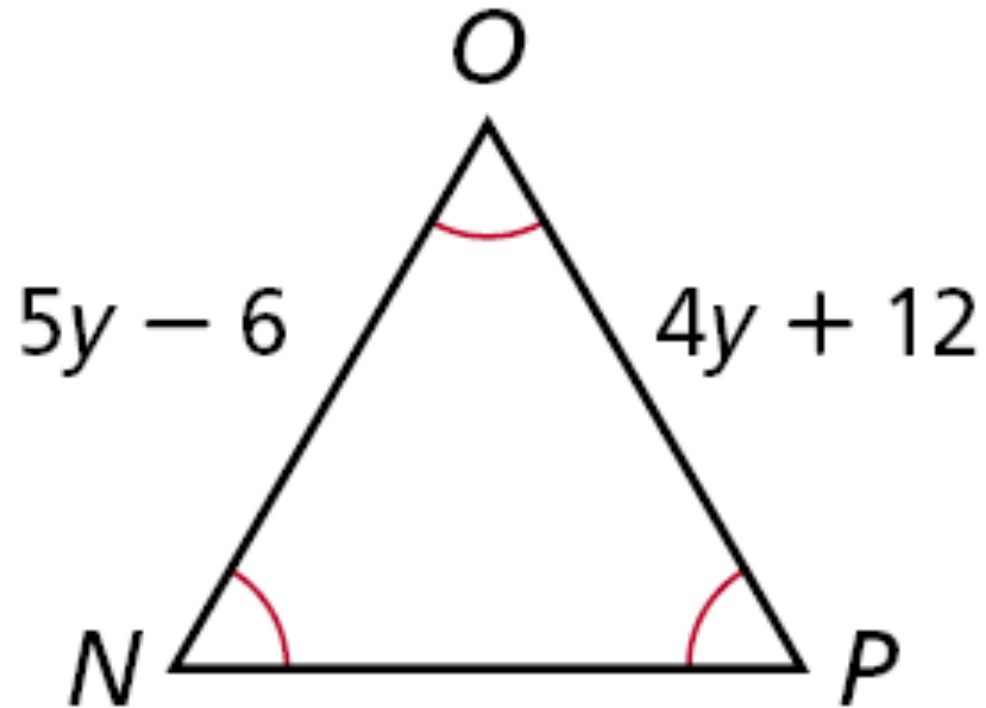
The length of  $\overline{YX}$  is 20 feet.

Explain why the length of  $\overline{YZ}$  is the same.



**Find the value of  $y$ .**

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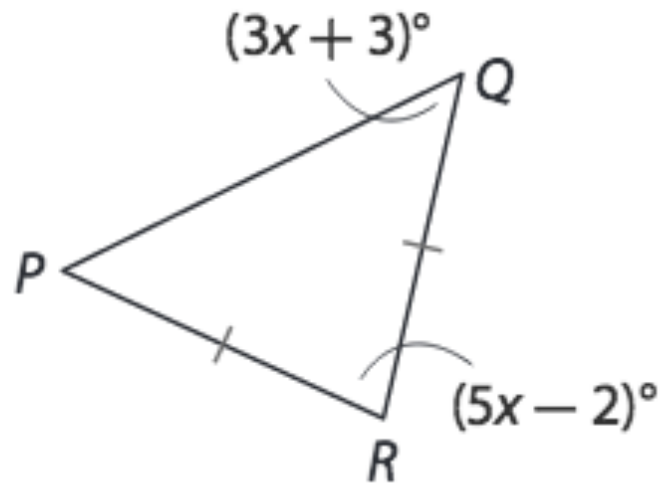


$$y = 18$$

# Your turn! pg. 1102 (5-8)

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5. Find  $m\angle P$ .



$$m\angle P = m\angle Q = (3x + 3)^\circ$$

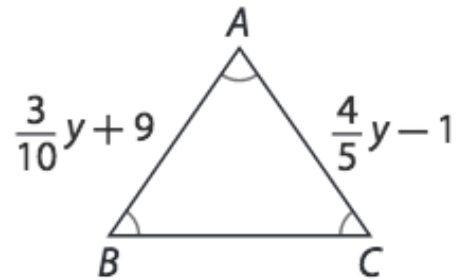
$$2(3x + 3) + (5x - 2) = 180$$

$$x = 16$$

$$m\angle P = (3x + 3)^\circ = (3(16) + 3)^\circ = 51^\circ$$



6. Katie's tutorial service is going so well that she is having shirts made with the equilateral triangle emblem. She has given the t-shirt company these dimensions. What is the length of each side of the triangle in centimeters?



$$\overline{AB} \cong \overline{AC} \quad \Rightarrow \quad AB = AC$$

$$\frac{3}{10}y + 9 = \frac{4}{5}y - 1 \quad \Rightarrow \quad 20 = y$$

$$\text{Therefore, } \frac{3}{10}y + 9 = \frac{3}{10}(20) + 9 = 6 + 9 = 15$$

**The length of each side is 15 cm.**

- 7. Discussion** Consider the vertex and base angles of an isosceles triangle. Can they be right angles? Can they be obtuse? Explain.

The vertex angle of an isosceles triangle can be acute, right, or obtuse as long as its measure is less than  $180^\circ$ . The base angles of an isosceles triangle can only be acute, meaning they have a measurement less than  $90^\circ$ . because otherwise they would cause the sum of the base angles to be  $\geq 180^\circ$  before adding in the third angle, which contradicts the Triangle Sum Theorem.

- 8. Essential Question Check-In** Discuss how the sides of an isosceles triangle relate to its angles.

**The legs of an isosceles triangle are opposite from the base angles and because the base angles are congruent, the legs are also congruent because of the Converse of the Isosceles Triangle Theorem.**

# Homework

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- pg. 1104-1108 (4-10, 12, 13, 19, 20)]
- **\*\*\*You don't need to rip this one out!!! Too many pages.\*\*\***