

Warmup 2/ (# of touchdowns the  
**Chiefs scored on Sunday)** Created by Mr. Lischwe

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- ▶ **Warmup – Compare Homework answers with your table!!!**



# Worksheet Answers

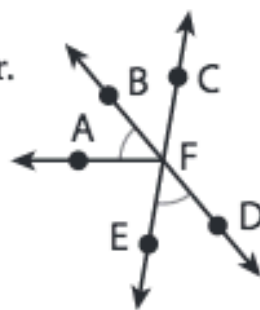
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- ▶ 1.  $a = 60, b = 120, c = 120$
- ▶ 2.  $a = 90, b = 90, c = 50$
- ▶ 3.  $a = 77, b = 52, c = 77, d = 51$
- ▶ 4.  $a = 60, b = 120, c = 120, d = 115, e = 65,$   
 $f = 115, g = 125, h = 55, i = 125$
- ▶ 5.  $a = 90, b = 163, c = 17, d = 110, e = 70$
- ▶ 6. This is a linear pair, so the measures should add up to  $180^\circ$ . But  $129 + 41 = 170$ .



**Given:**  $m\angle AFB = m\angle EFD = 50^\circ$

Points  $B, F, D$  and points  $E, F, C$  are collinear.



1. Determine whether each pair of angles is a pair of vertical angles, a linear pair of angles, or neither. Select the correct answer for each lettered part.

A. $\angle BFC$ and $\angle DFE$	<input checked="" type="radio"/> Vertical	<input type="radio"/> Linear Pair	<input type="radio"/> Neither
B. $\angle BFA$ and $\angle DFE$	<input type="radio"/> Vertical	<input type="radio"/> Linear Pair	<input checked="" type="radio"/> Neither
C. $\angle BFC$ and $\angle CFD$	<input type="radio"/> Vertical	<input checked="" type="radio"/> Linear Pair	<input type="radio"/> Neither
D. $\angle AFE$ and $\angle AFC$	<input type="radio"/> Vertical	<input checked="" type="radio"/> Linear Pair	<input type="radio"/> Neither
E. $\angle BFE$ and $\angle CFD$	<input checked="" type="radio"/> Vertical	<input type="radio"/> Linear Pair	<input type="radio"/> Neither
F. $\angle AFE$ and $\angle BFC$	<input type="radio"/> Vertical	<input type="radio"/> Linear Pair	<input checked="" type="radio"/> Neither

2. Find  $m\angle AFE$ .

$$m\angle AFB + m\angle AFE + m\angle EFD = 180^\circ$$

$$50^\circ + m\angle AFE + 50^\circ = 180^\circ$$

$$m\angle AFE = 80^\circ$$

3. Find  $m\angle DFC$ .

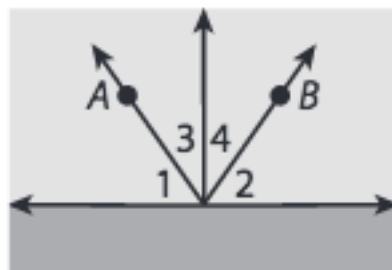
$$m\angle EFB = m\angle AFB + m\angle AFE = 80^\circ + 50^\circ = 130^\circ$$

$$m\angle DFC = m\angle EFB, \text{ so } m\angle DFC = 130^\circ$$

4. Find  $m\angle BFC$ .

$$m\angle BFC = m\angle EFD = 50^\circ$$

5. **Represent Real-World Problems** A sprinkler swings back and forth between  $A$  and  $B$  in such a way that  $\angle 1 \cong \angle 2$ ,  $\angle 1$  and  $\angle 3$  are complementary, and  $\angle 2$  and  $\angle 4$  are complementary. If  $m\angle 1 = 47.5^\circ$ , find  $m\angle 2$ ,  $m\angle 3$ , and  $m\angle 4$ .



$$\angle 1 \cong \angle 2, \text{ so } m\angle 2 = 47.5^\circ$$

$$\angle 1 \text{ and } \angle 3 \text{ are complementary, so } m\angle 3 = 90 - 47.5 = 42.5^\circ$$

$$\angle 2 \text{ and } \angle 4 \text{ are complementary, so } m\angle 4 = 90 - 47.5 = 42.5^\circ$$

6. If an angle is acute, then the measure of its complement must be greater than the measure of its supplement.

**False. The measure of an acute angle is less than  $90^\circ$ , so the measure of its complement will be less than  $90^\circ$  and the measure of its supplement will be greater than  $90^\circ$ . So, the measure of the supplement will be greater than the measure of the complement.**

7. A pair of vertical angles may also form a linear pair.

**False. Vertical angles do not share a common side.**

8. If two angles are supplementary and congruent, the measure of each angle is  $90^\circ$ .

**True**

9. If a ray divides an angle into two complementary angles, then the original angle is a right angle.

**True**

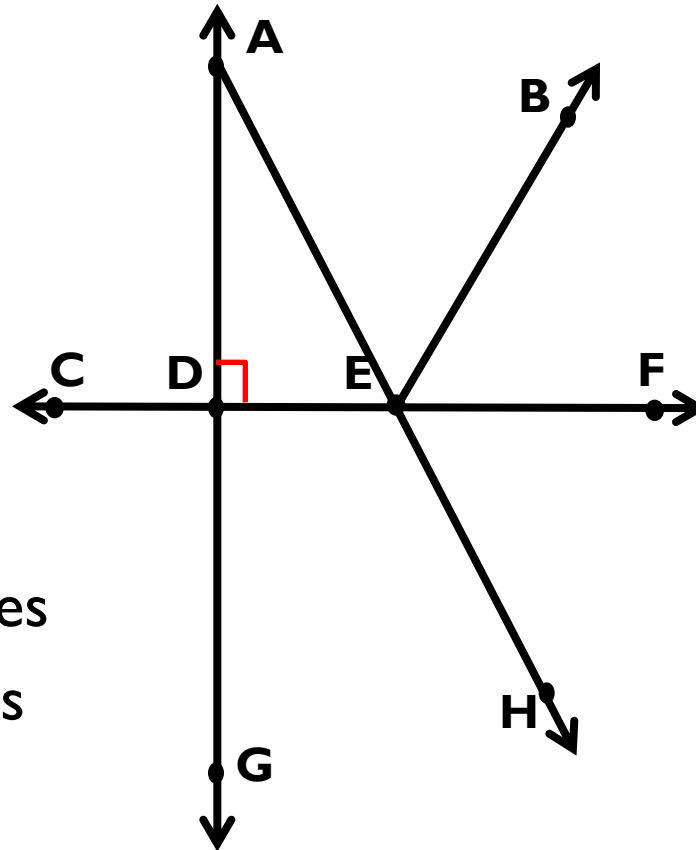
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# Summary:

Name an example of each of the following:

- ▶ An acute angle
- ▶ An obtuse angle
- ▶ A right angle
- ▶ A straight angle
- ▶ A pair of adjacent angles
- ▶ A pair of vertical angles
- ▶ A pair of complementary angles
- ▶ A pair of supplementary angles
- ▶ A pair of congruent angles



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# Angles formed by Parallel Lines

## Objectives:

- ▶ Given one angle measure, find ALL angles formed by 2 parallel lines
- ▶ Identify special angle pairs
- ▶ Use special angle pair rules to find angle measures



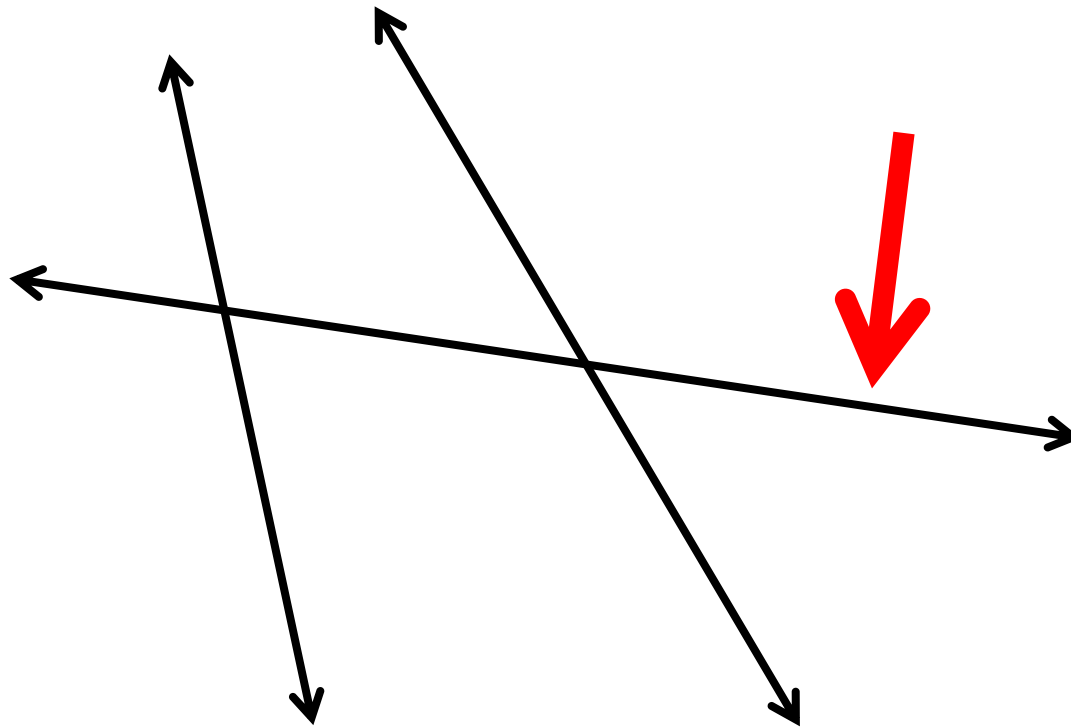
is parallel to



is not parallel to



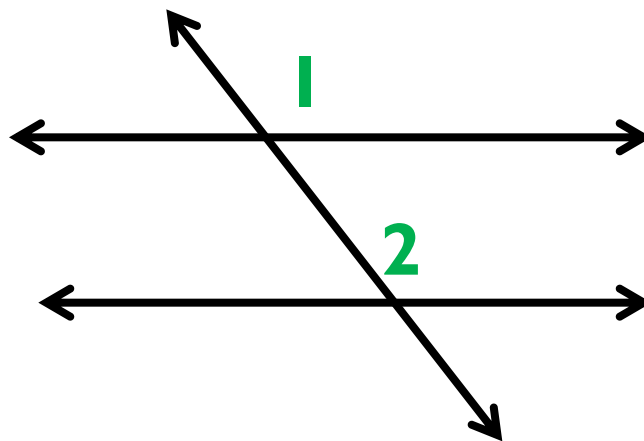
- 
- ▶ **TRANSVERSAL**: A line that intersects two coplanar lines.



# Corresponding Angles

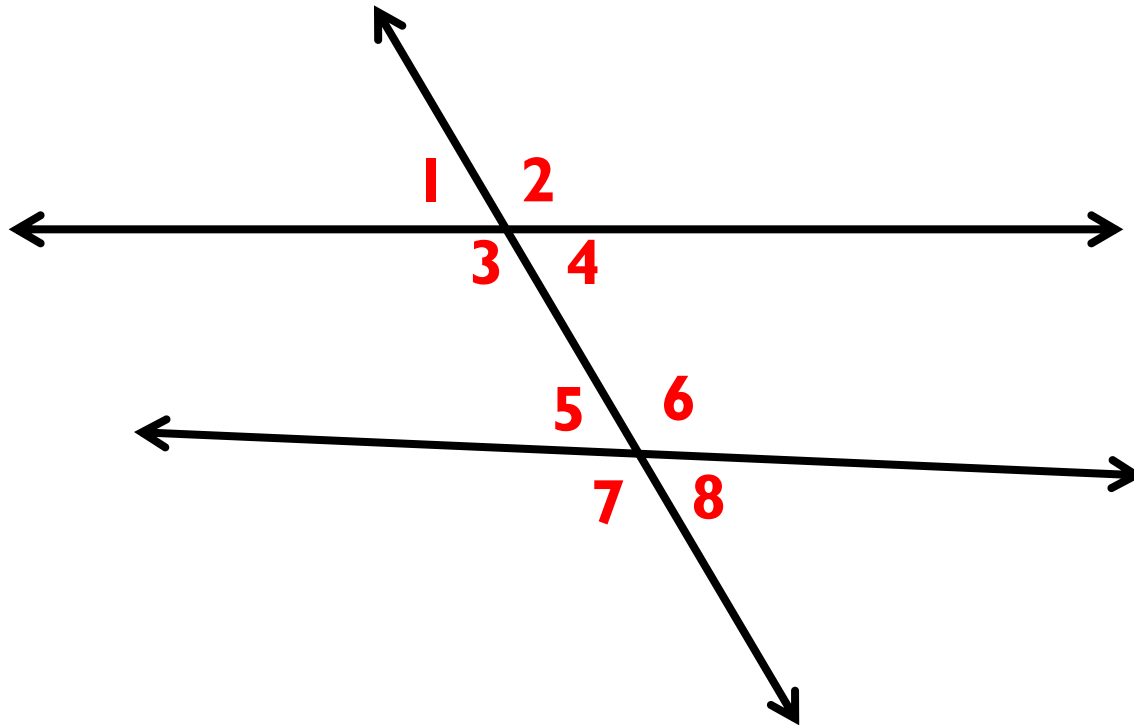
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- ▶ Two angles that are in the same “position” but on different lines are called **corresponding**.



# New terminology

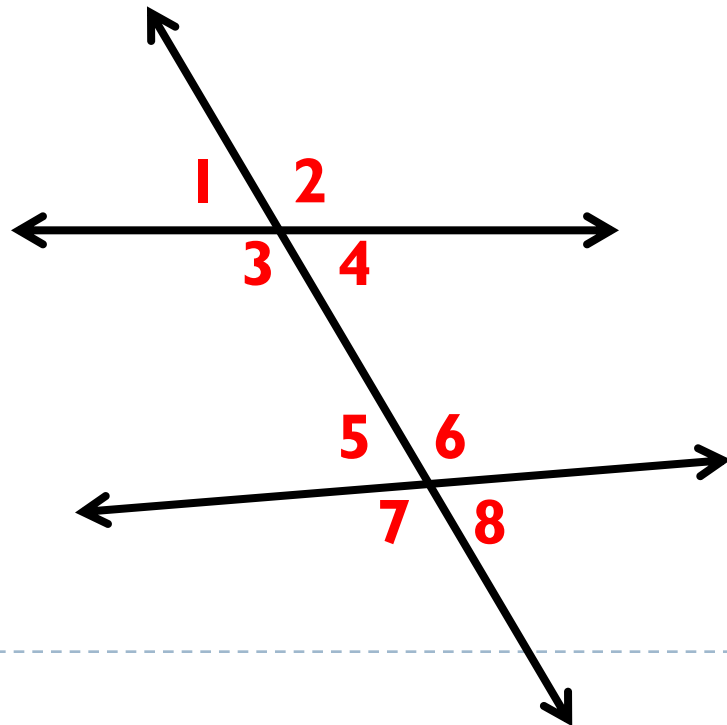
- ▶ Which angles would you say are **interior** angles?  $3, 4, 5, 6$
- ▶ Which angles would you say are **exterior** angles?  $1, 2, 7, 8$



# New terminology

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- ▶ **Interior: between the lines**
- ▶ **Exterior: outside the lines**
- ▶ **Alternate: opposite sides of the transversal**
- ▶ **Same-side: same side of the transversal**



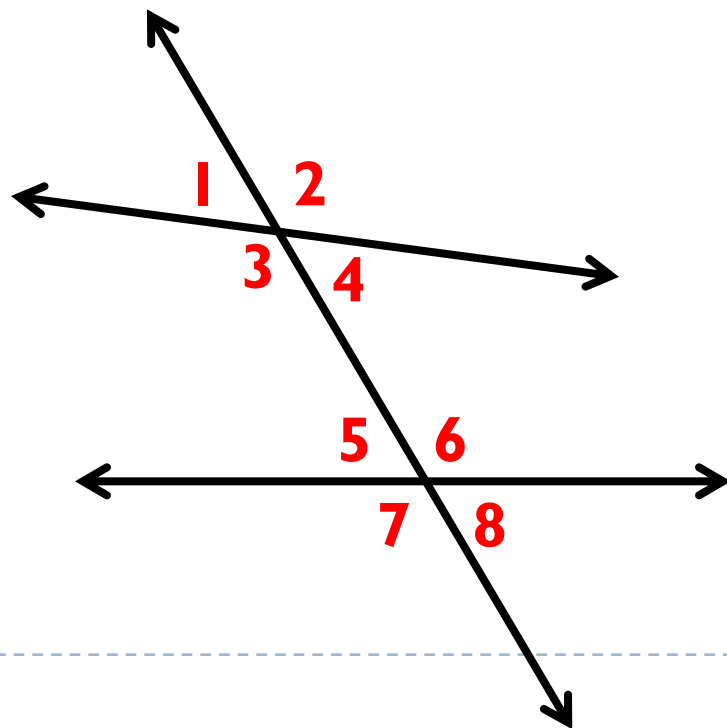
Give me an example of:

- A pair of **alternate interior** angles
  - A pair of **same-side interior** angles
  - A pair of **alternate exterior** angles
-

# IN YOUR NOTES!

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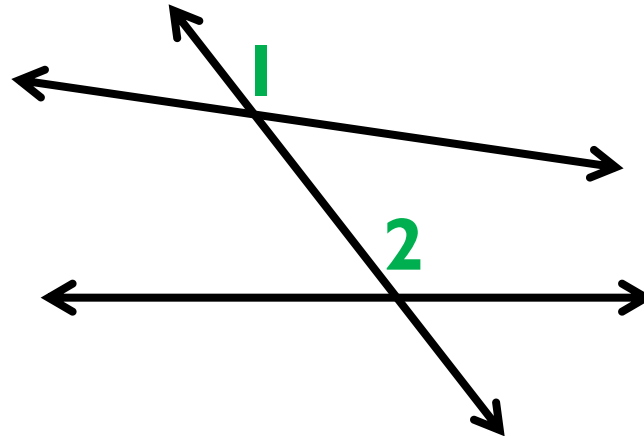
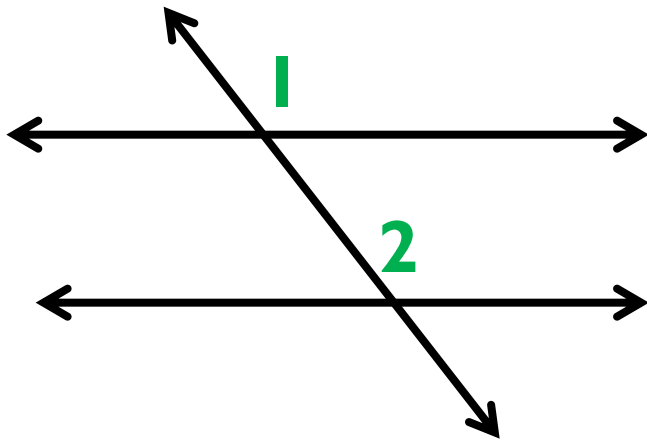
- ▶ **Alternate Interior:**  $\angle 4$  and  $\angle 5$ ,  $\angle 3$  and  $\angle 6$
- ▶ **Same-side Interior:**  $\angle 3$  and  $\angle 5$ ,  $\angle 4$  and  $\angle 6$
- ▶ **Alternate Exterior:**  $\angle 1$  and  $\angle 8$ ,  $\angle 2$  and  $\angle 7$
- ▶ **Corresponding:**  $\angle 1$  and  $\angle 5$ ,  $\angle 2$  and  $\angle 6$ ,  $\angle 3$  and  $\angle 7$ ,  $\angle 4$  and  $\angle 8$



# Corresponding Angles

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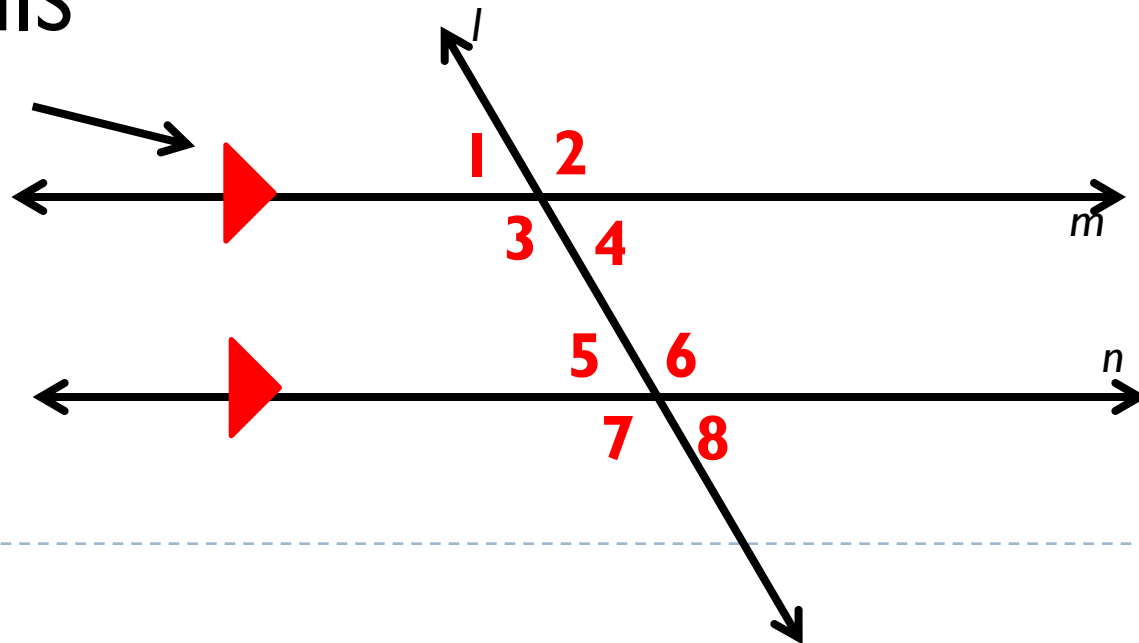
- ▶ If the lines are parallel, corresponding angles will be congruent!!!



# DISCUSS WITH YOUR GROUP:

- ▶ **If lines  $m$  and  $n$  are parallel**, which angles are congruent to each other?
- ▶ Discuss in groups:
  - ▶ Which angles do you think are congruent?
  - ▶ Why do you think they are congruent?
  - ▶ Does your group all agree or not?

WHAT IS THIS  
SYMBOL????



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▶ Same Side Interior Angles Postulate:

▶ If two parallel lines are cut by a transversal, then the pairs of same-side interior angles are supplementary

▶ Corresponding Angles Theorem

▶ If two parallel lines are cut by a transversal, then the pairs of corresponding angles have the same measure





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▶ **Alternate Interior Angles Theorem:**

- ▶ If two parallel lines are cut by a transversal, then **the pairs of alternate interior angles have the same measure**

▶ **Alternate Exterior Angles Theorem:**

- ▶ If two parallel lines are cut by a transversal, then **the pairs of alternate exterior angles have the same measure**



# IN YOUR BINDER

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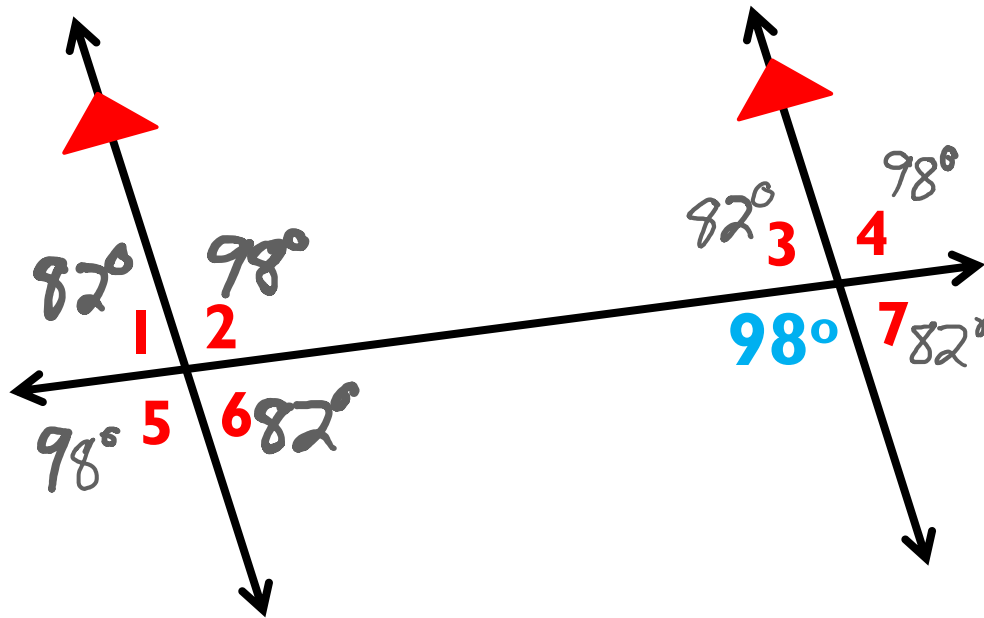
- ▶ **IF THE LINES ARE PARALLEL:**
  - ▶ Alternate Interior: congruent
  - ▶ Alternate Exterior: congruent
  - ▶ Same-side Interior: supplementary
  - ▶ Corresponding: congruent



# Whiteboard Practice

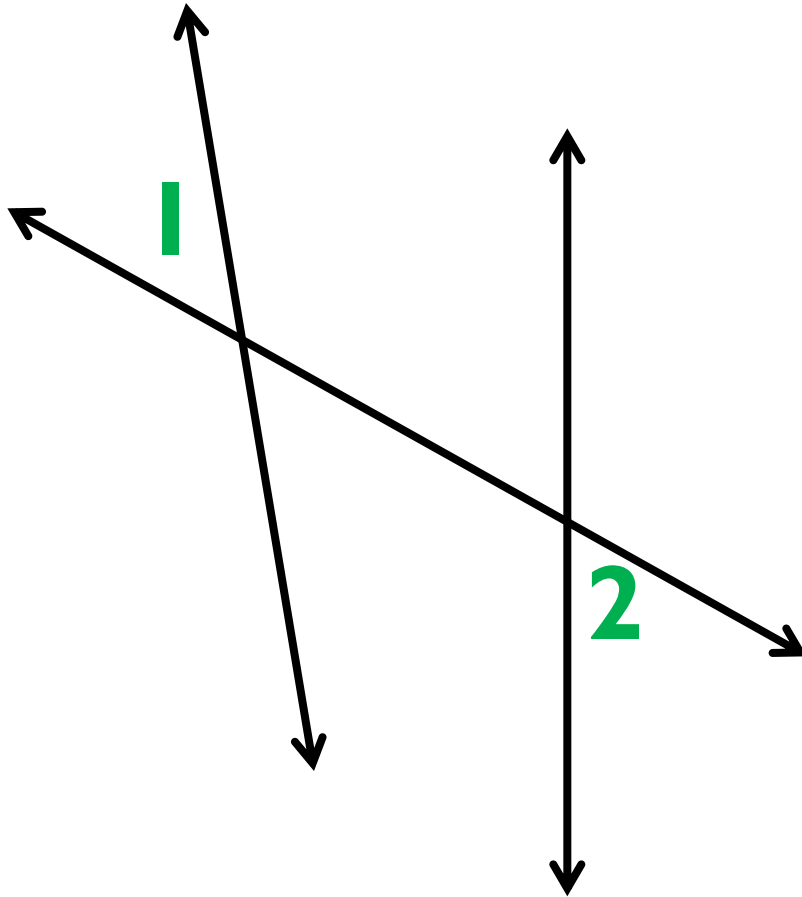
You can always refer back to these slides on my website

- 
- ▶ One angle measure is given. Find the measures of **ALL** other angles.



# Which type of angle?

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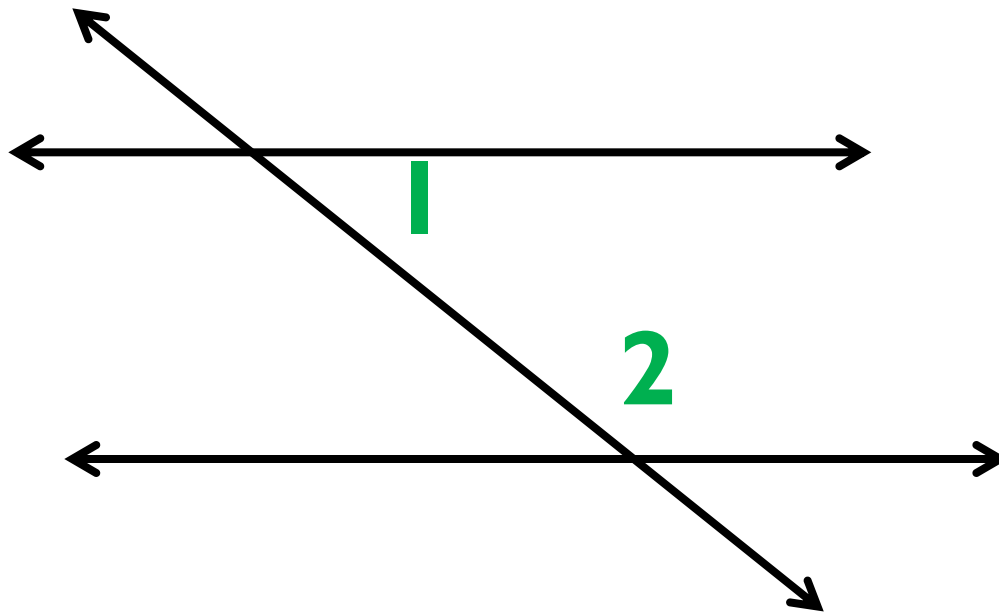


Alternate  
Exterior



Which type of angle?

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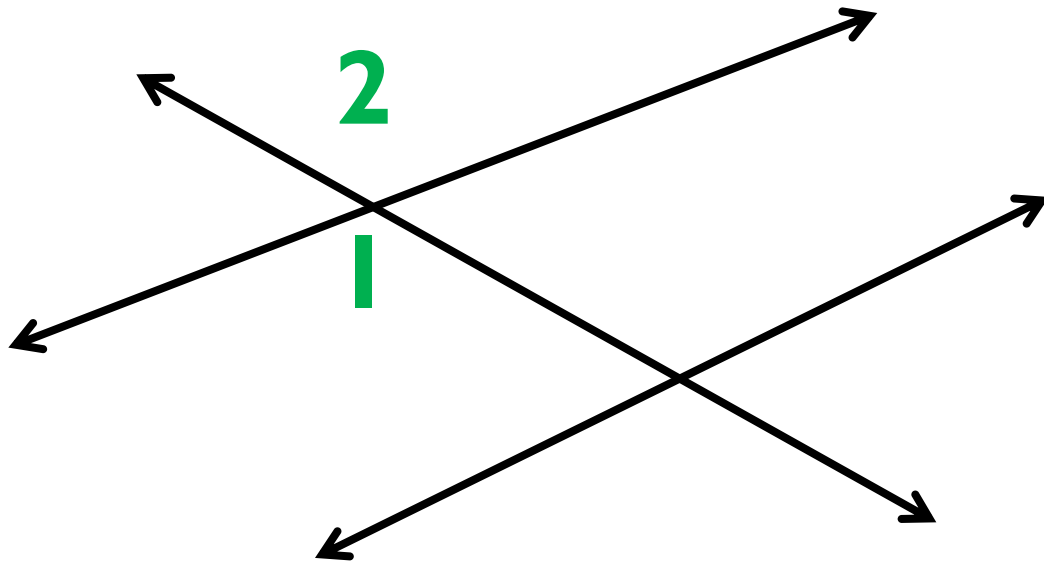


*Corresponding*



Which type of angle?

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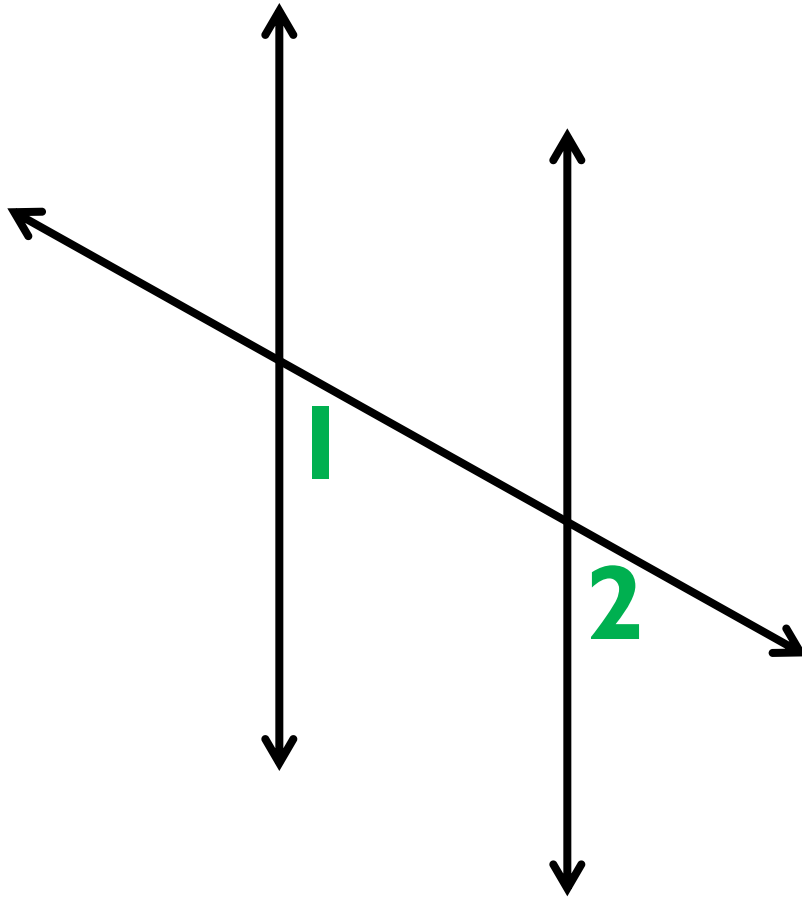


Vertical



Which type of angle?

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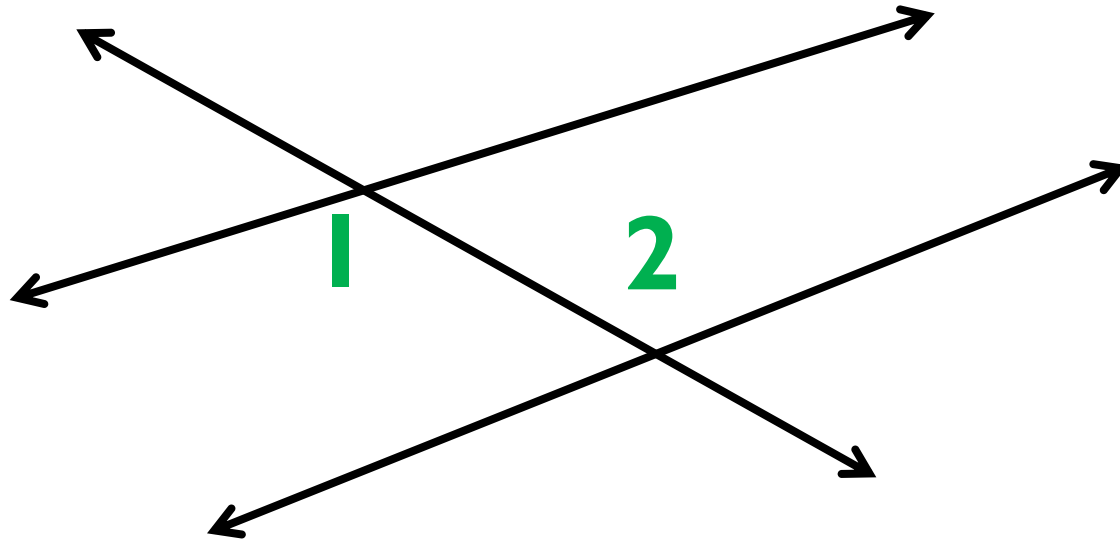
*Corresponding*





Which type of angle?

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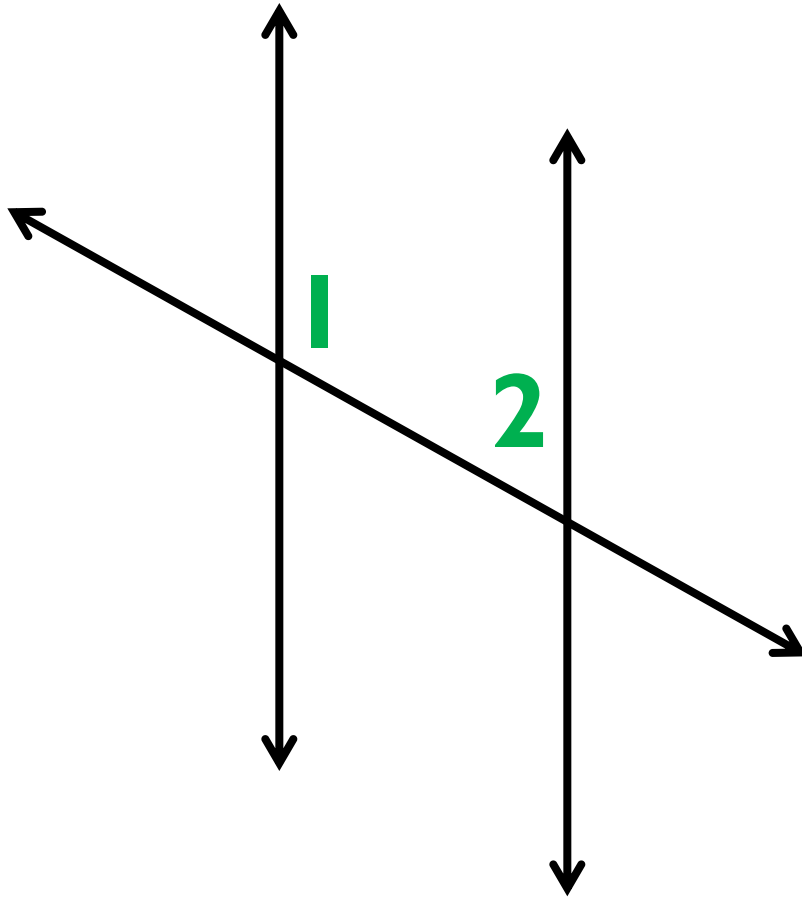


*Alternate  
Interior*



# Which type of angle?

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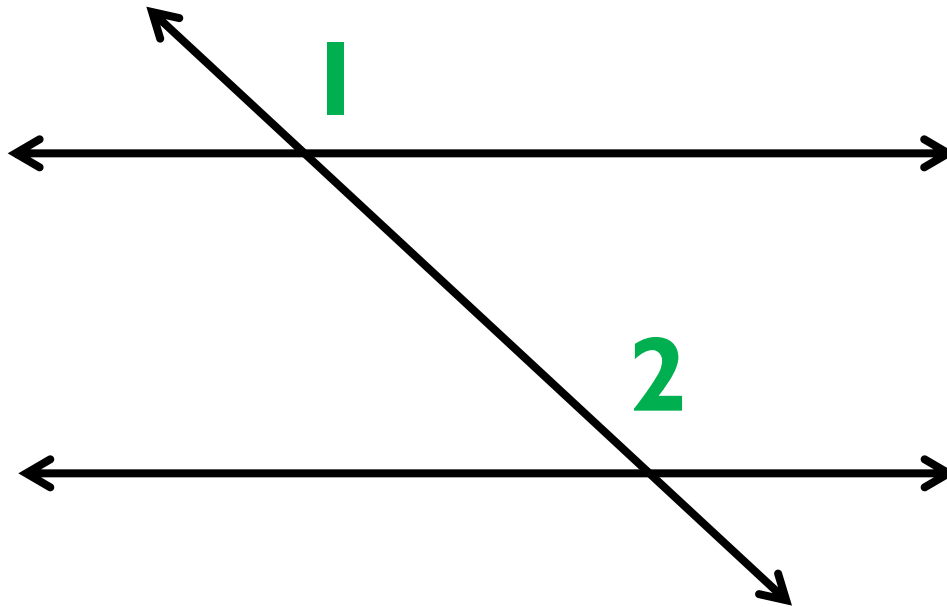


Same-Side  
Interior



Which type of angle?

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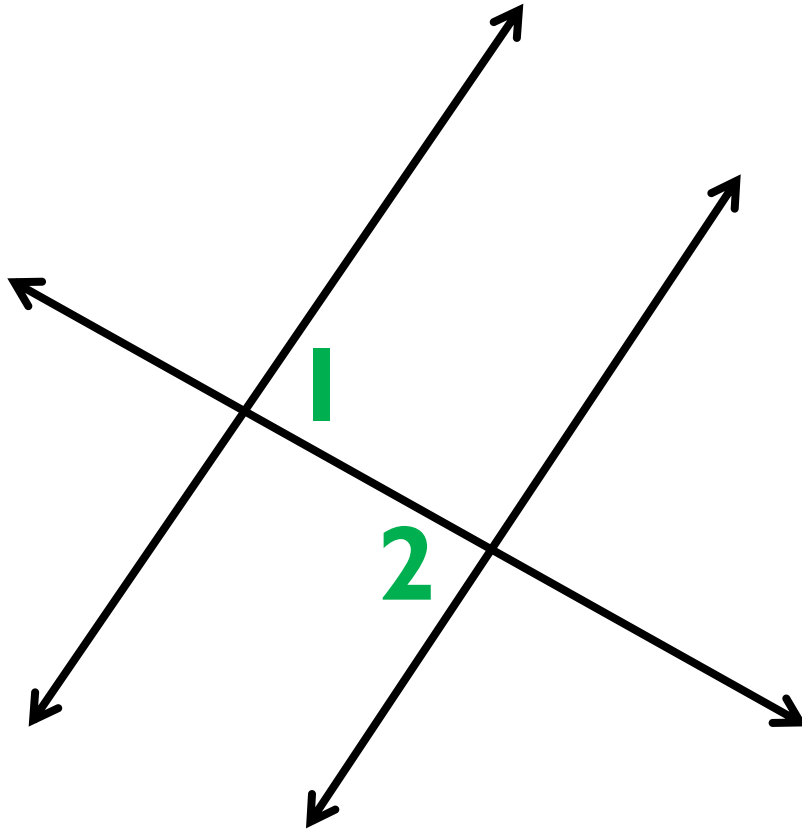


*Corresponding*



Which type of angle?

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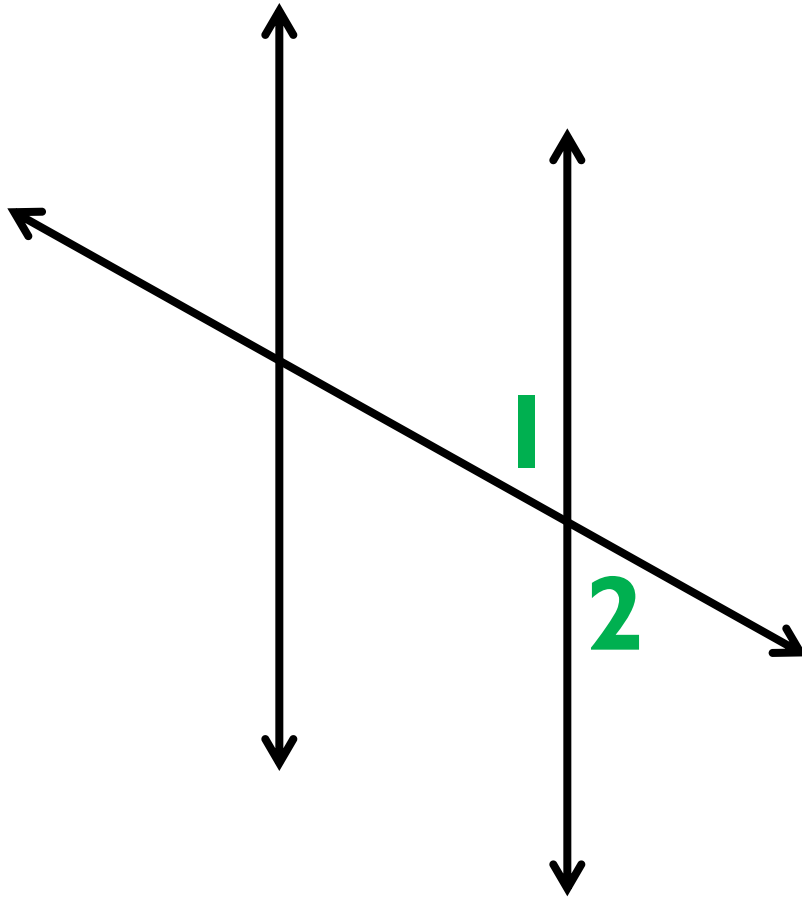


Alternate  
Interior



# Which type of angle?

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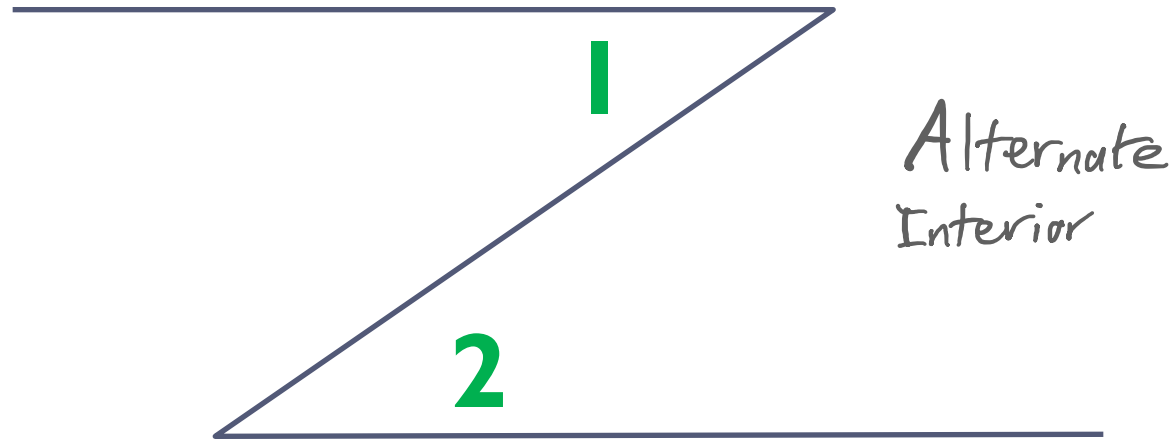


Vertical



# Which type of angle?

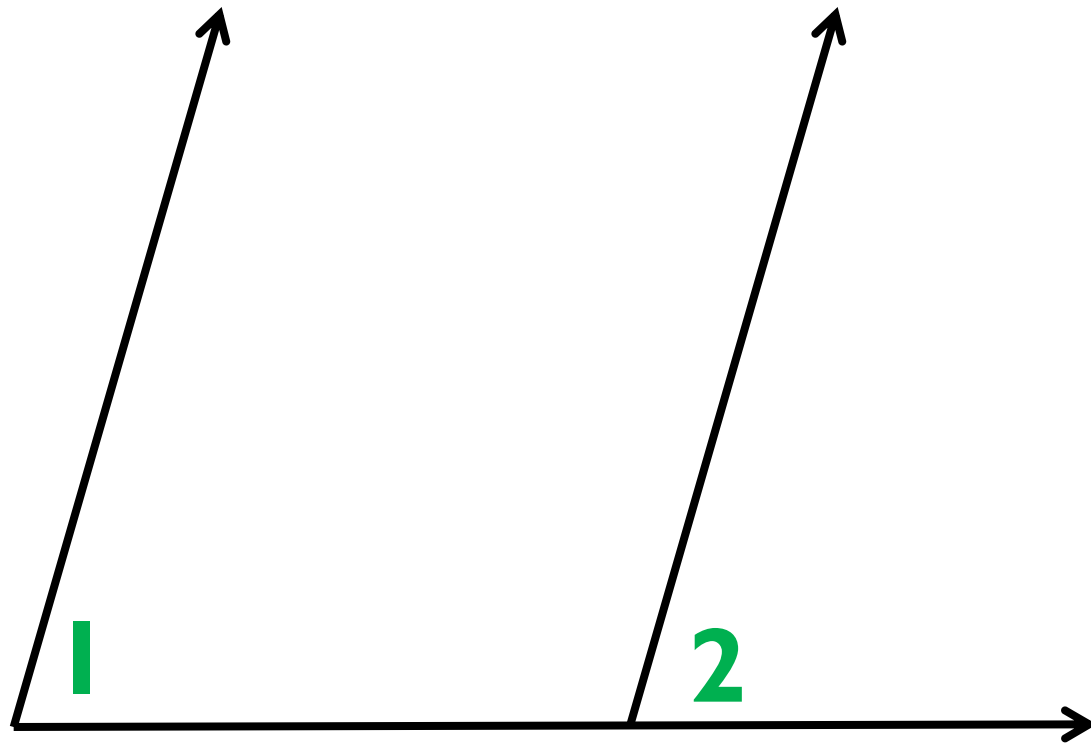
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Which type of angle?

---

**Corresponding**



Which type of angle?

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**Same-side interior**

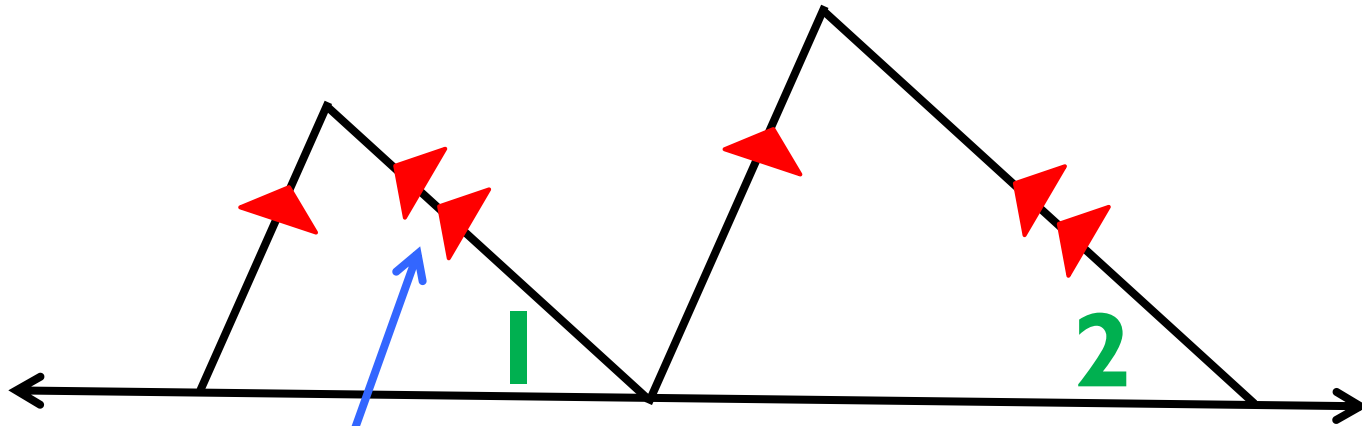




Which type of angle?

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# Corresponding

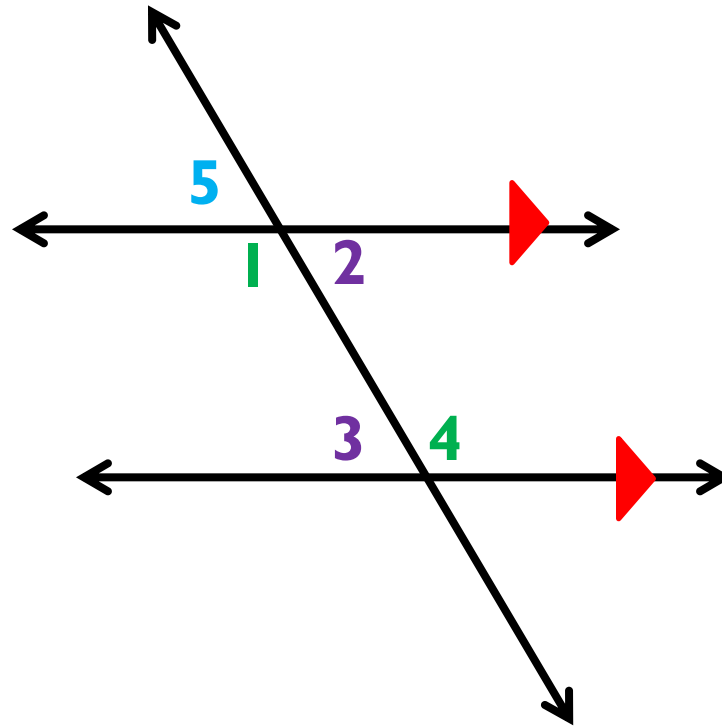


WHY ARE THERE TWO  
ARROWS???

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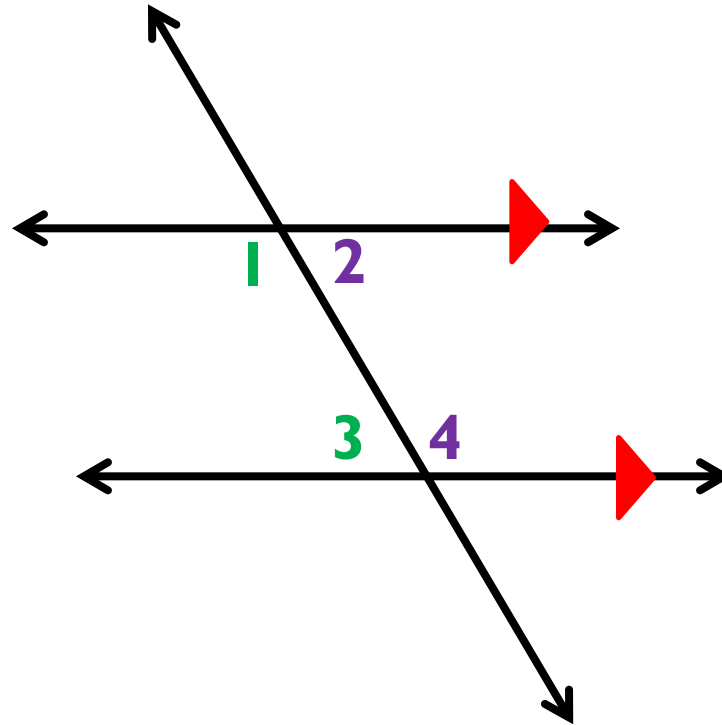
- 
- ▶ What is **ALWAYS** true about alternate interior angles when two parallel lines are cut by a transversal?



**They are congruent**

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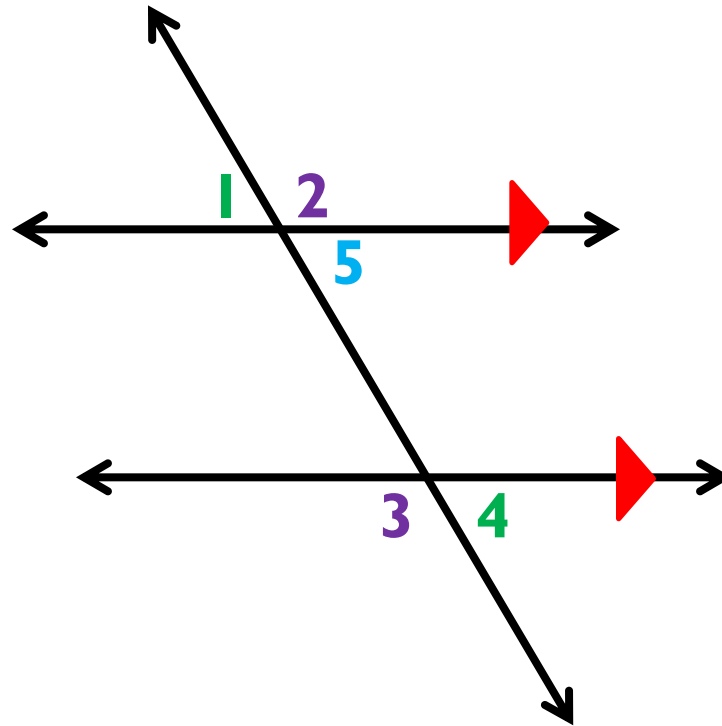
- 
- ▶ What is **ALWAYS** true about same-side interior angles when two parallel lines are cut by a transversal?



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▶ **They are supplementary**

- 
- ▶ What is **ALWAYS** true about alternate exterior angles when two parallel lines are cut by a transversal?

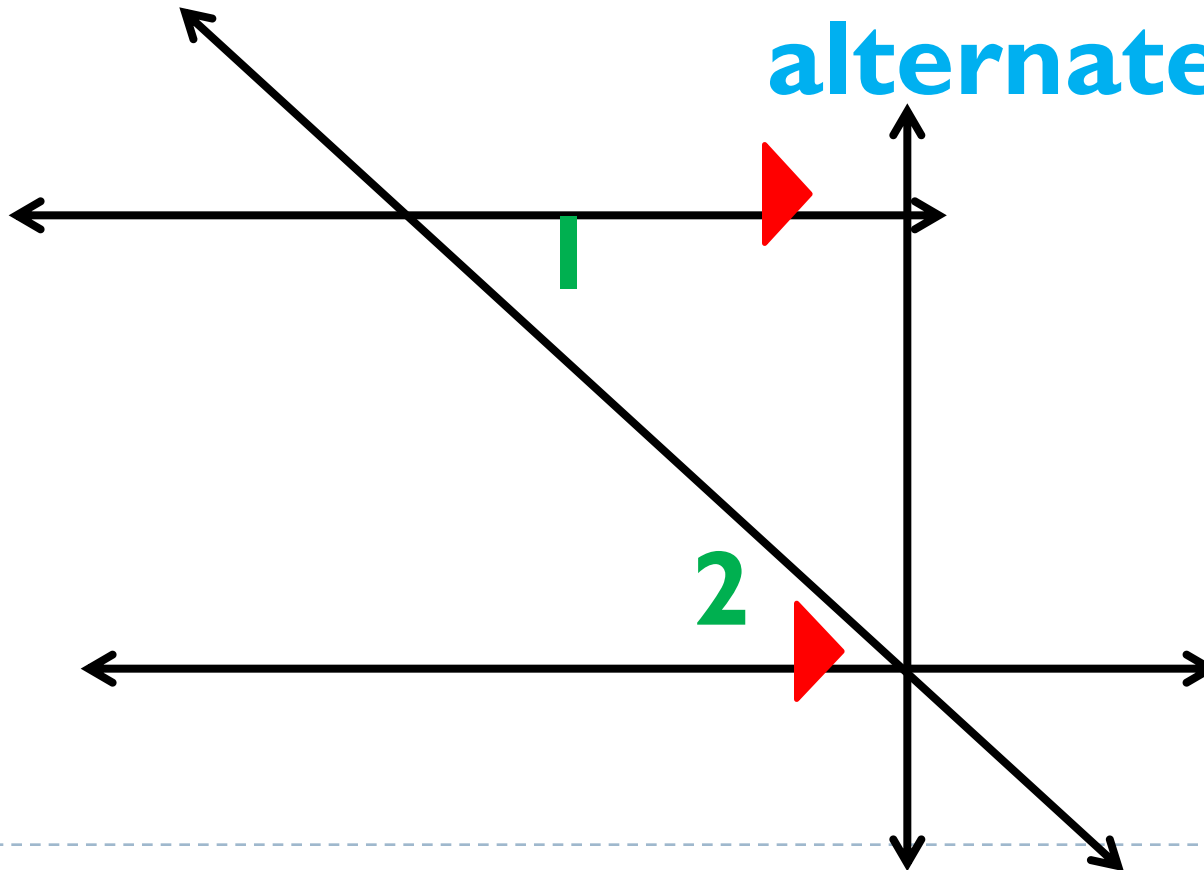


**They are congruent**

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If the measure of angle 1 is 47 degrees, what is the  
measure of angle 2? **HOW DO YOU KNOW?**

$m\angle 2 = 47^\circ$ ; they are  
alternate interior



# With algebra...

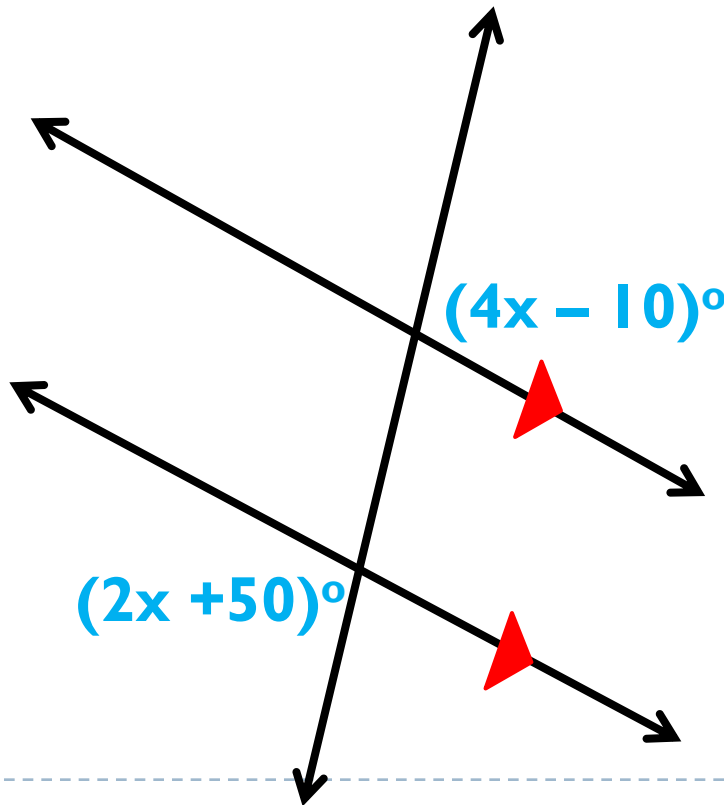
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- ▶ Find the value of  $x$ .

**Alt. Ext: congruent**

$$2x + 50 = 4x - 10$$

$$x = 30$$



# With algebra...

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- ▶ Find the measure of both angles.

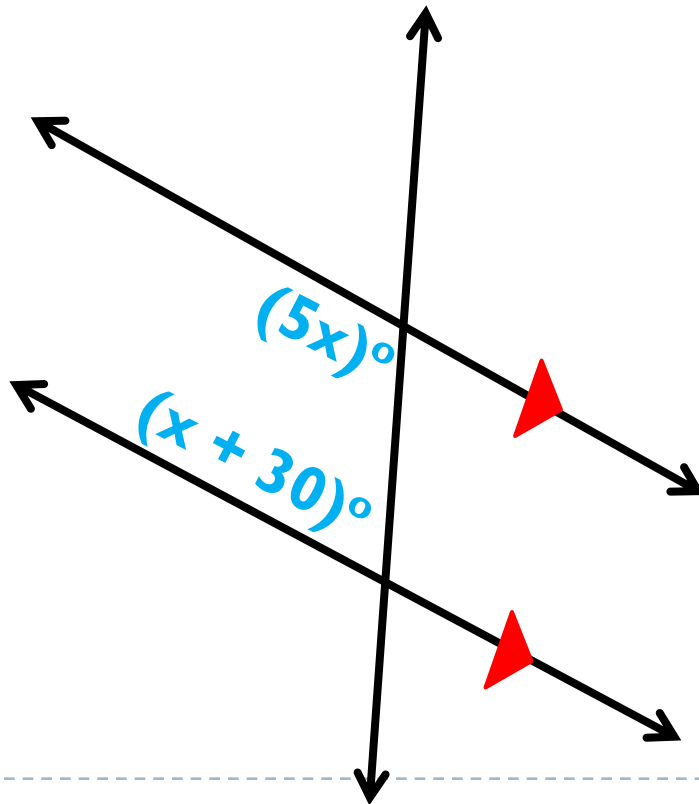
**Same-side interior:  
supplementary**

$$(5x) + (x + 30) = 180$$

$$6x + 30 = 180$$

$$x = 25$$

$$55^\circ, 125^\circ$$



# Homework

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## ▶ Worksheet

