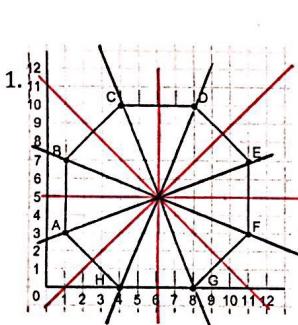


Describe any rotational or line symmetry for each figure in the coordinate plane.

around (6,5)



Rotations:

90°, 180°, 270°

(It is not quite regular)

Reflections: (8 lines)

$$y=5$$

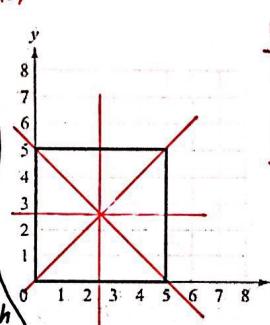
$$y=x-1$$

$$x=6$$

$$y=-x+11$$

For the rest, point-slope form is easiest. All go through (6,5)

$$\cdot y-5 = \frac{2}{5}(x-6) \quad | \quad y-5 = -\frac{2}{5}(x-6) \quad | \quad y-5 = \frac{5}{2}(x-6) \quad | \quad y-5 = -\frac{5}{2}(x-6)$$



Rotations:

90°, 180°, 270°
around (2.5, 2.5)

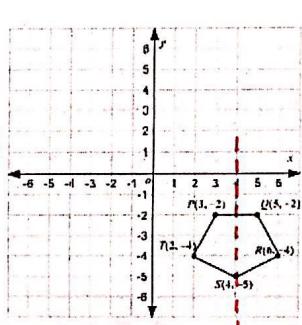
Reflections: (4 lines)

$$x=2.5$$

$$y=2.5$$

$$y=x$$

$$y=-x+5$$



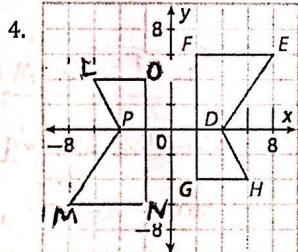
Rotations:

90°, 180°, 270°
around (5, 2)

Reflections: (1 line)

No rotations
(It is not regular)

Reflections: (1 line)
 $x=4$

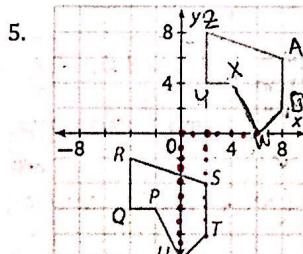


180° Rotation

OR

Reflect across x-axis,
then reflect across y-axis

$$\text{DEFGH} \cong \text{PMNLO}$$

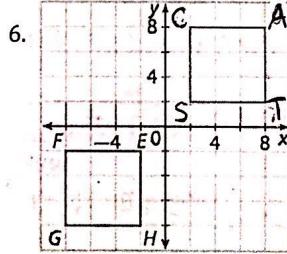


Translation:

$$(x, y) \rightarrow (x-6, y-10)$$

$$(x-6, y-10)$$

$$\text{ABWXY} \cong \text{STUPQR}$$



Translation: $(x, y) \rightarrow (x-10, y-10)$

$$\text{CATS} \cong \text{FEHG}$$

OR

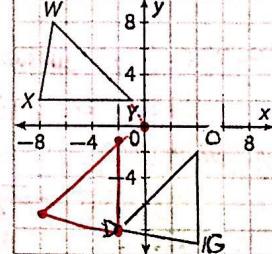
180° Rotation around (0,0)

$$\text{CATS} \cong \text{HGFE}$$

OR

Reflect across $y = -x$

$$\text{CATS} \cong \text{FGHE}$$



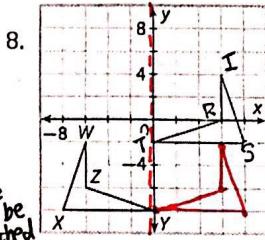
Rotation: 90° CCW around (0,0)
then Translation: $(x, y) \rightarrow (x+6, y-1)$

$$\text{AWXY} \cong \text{ADGO}$$

$$\begin{aligned} \angle W &\cong \angle D & \overline{WX} &\cong \overline{DG} \\ \angle X &\cong \angle G & \overline{XY} &\cong \overline{GO} \\ \angle Y &\cong \angle O & \overline{WY} &\cong \overline{DO} \end{aligned}$$

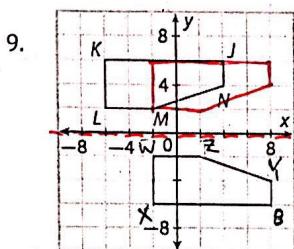
Congruent
parts

- Find a sequence of transformations that maps one figure to the other.
- Write a congruency statement (i.e. $\triangle ABC \cong DEF$). Order of the letters matters!
- Identify congruent parts.



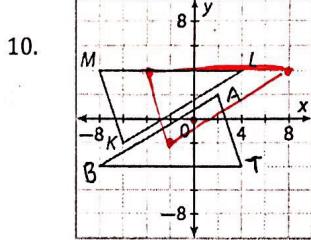
These could be switched
Reflect across y-axis
then
Translate $(x, y) \rightarrow (x, y + 6)$

$$WXYZ \cong ISTR$$



Translate $(x, y) \rightarrow (x + 4, y)$
then
Reflect across x-axis

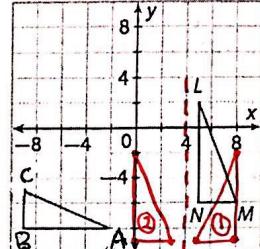
$$JKLMN \cong BXWZY$$



These could be switched
Rotate 180° around (0,0)
then
Translate $(x, y) \rightarrow (x - 4, y)$
OR
Rotate 180° around (-2,0)

$$\triangle ABAT \cong \triangle LKM$$

Challenge!

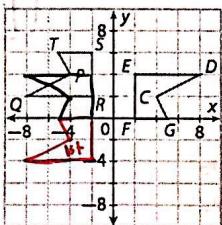


Possible Answer

- Rotate 90° CCW around (0,0)
- Reflect across x = 4
- Translate $(x, y) \rightarrow (x + 5, y + 3)$

12. **Draw Conclusions** Two students are trying to show that the two figures are congruent. The first student decides to map CDEFG to PQRST using a rotation of 180° around the origin, followed by the translation $(x, y) \rightarrow (x, y + 6)$. The second student believes the correct transformations are a reflection across the y-axis, followed by the vertical translation $(x, y) \rightarrow (x, y - 2)$. Are both students correct, is only one student correct, or is neither student correct?

Only the first student
is correct.



13. Which sequence of transformations does not map a figure onto a congruent figure? Explain

- A. Rotation of 180° about the origin, reflection across the x-axis, horizontal translation $(x, y) \rightarrow (x + 4, y)$
- B. Reflection across the y-axis, combined translation $(x, y) \rightarrow (x - 5, y + 2)$
- C. Rotation of 180° about the origin, reflection across the y-axis, dilation $(x, y) \rightarrow (2x, 2y)$
- D. Counterclockwise rotation of 90° about the origin, reflection across the y-axis, combined translation $(x, y) \rightarrow (x - 11, y - 12)$

* The image will not be congruent because
the dilation will make it bigger.