

Solving Equations – Challenge Worksheet

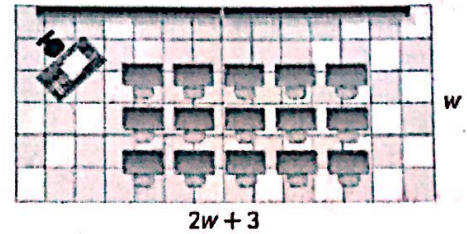
MP Persevere with Problems Solve $(x + 5)(x + 5) = 49$.
(Hint: There are two solutions.) (Use guess and check!)

$$\begin{aligned} x &= 2 & (7)(7) &= 49 \\ \text{or} & & & \\ x &= -12 & (-7)(-7) &= 49 \end{aligned}$$

MP Persevere with Problems A diagram of a room is shown. If the perimeter of the room is 78 feet, what is the area of the floor of the room? (Lesson 3)

$$\begin{aligned} (2w+3) + w + (2w+3) + w &= 78 \\ 6w + 6 &= 78 \\ 6w &= 72 \\ w &= 12 \end{aligned}$$

$$\begin{aligned} \text{length} &= 2 \cdot 12 + 3 \\ &= 27 \\ \text{width} &= 12 \\ 27 \cdot 12 &= 324 \\ \boxed{324 \text{ ft}^2} \end{aligned}$$



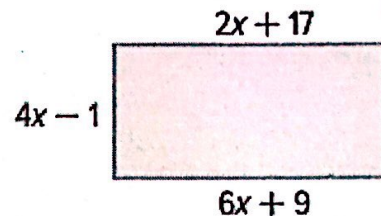
MP Persevere with Problems Find the area of the rectangle at the right.

$$\begin{aligned} 2x+17 &= 6x+9 \\ 17 &= 4x+9 \\ 8 &= 4x \\ 2 &= x \end{aligned}$$

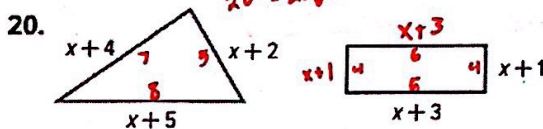
$$\begin{aligned} 2 \cdot 2 + 17 &= 21 \\ 4 \cdot 2 - 1 &= 7 \end{aligned}$$

$$\frac{21}{7} = 3$$

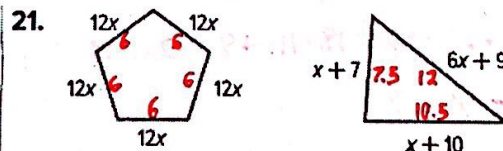
$$\boxed{147 \text{ units}^2}$$



MP Reason Abstractly Write an equation to find the value of x so that each pair of polygons has the same perimeter. Then solve.



$$\begin{aligned} (x+4) + (x+2) + (x+5) &= (x+1) + (x+3) + (x+1) + (x+3) \\ 3x+11 &= 4x+8 \\ 11 &= x+8 \\ \boxed{3} &= x \end{aligned}$$



$$\begin{aligned} 5(12x) &= (x+7) + (6x+9) + (x+10) \\ 60x &= 8x+26 \\ 52x &= 26 \\ \boxed{x} &= \frac{1}{2} \end{aligned}$$

You and your friend both bought some gum. Your friend spent three times as much as you did. Altogether, you spent \$4.80. How much did you each spend on gum?

$$\begin{aligned} \text{You} &= x \\ \text{Friend} &= 3x \end{aligned}$$

$$\begin{aligned} x + 3x &= 4.80 \\ 4x &= 4.80 \\ x &= 1.20 \end{aligned}$$

$$\begin{aligned} \text{You} &= \$1.20 \\ \text{Friend} &= \$3.60 \end{aligned}$$

Solve each equation.

1) $4\frac{1}{3}x + 16 = 2\frac{2}{3}x + 21$

$$\frac{13}{3}x + 16 = \frac{8}{3}x + 21$$

$$\frac{5}{3}x = 5$$

$$x = 3$$

2) $\frac{12}{2}x + 12 = \frac{3}{4}x + 8$

$$12 = \frac{1}{4}x + 8$$

$$4 = \frac{1}{4}x$$

$$x = 16$$

3) $\frac{5}{6}x + 16 = -\frac{1}{4}x - 10$

$$\frac{10}{12}x + 16 = -\frac{3}{12}x - 10$$

$$\frac{13}{12}x + 16 = -10$$

$$\frac{13}{12}x = -26$$

$$x = -24$$

4) $\frac{1}{3}x + \frac{7}{6} = \frac{3}{4}x + \frac{2}{8}$ $\times 24 \rightarrow 8x + 28 = 18x + 6$

$$\frac{8}{12}x + \frac{28}{6} = \frac{9}{12}x + \frac{2}{3}$$

$$\frac{22}{3} = 10x$$

$$2.2 = x$$

$$\frac{7}{6} = \frac{5}{12}x + \frac{2}{3}$$

$$\frac{28}{24} = \frac{5}{12}x + \frac{6}{24}$$

$$\frac{22}{24} = \frac{5}{12}x$$

$$x = \frac{11}{5} \text{ or } 2\frac{1}{5} \text{ or } 2.2$$

5) $8(x - 2) + 3(2x + 3) = 3(x - 6)$

$$8x - 16 + 6x + 9 = 3x - 18$$

$$14x - 7 = 3x - 18$$

$$11x - 7 = -18$$

$$11x = -11$$

$$x = -1$$

6) $4 - 2x - 6x + 3 = 3x + 12 - 11x$

$$7 - 8x = -8x + 12$$

$$7 = 12$$

$$\text{No Solution}$$

7) $-3(2x - 5) + 7x - 14 + x - 4 + 2(10 + 2x) = 18 - 11x + 4(2 - x + 4x) - 0.5x + \frac{1}{2}x - 19$

$$-6x + 15 + 7x - 14 + x - 4 + 20 + 4x = 18 - 11x + 8 + 12x - 19$$

$$6x + 17 = x + 7$$

$$5x = -10$$

$$x = -2$$

I am thinking of a number. If I multiply that number by four, or divide that number by four, or add four to that number, or subtract four from that number, I would get four new numbers. When I add those four new numbers together, I get 400. What number am I thinking of? (For example, if I was thinking of the number 12, my four new numbers would be 48, 3, 16, and 8. The sum of those is 75. So 12 is not my number.)

$$4x + \frac{x}{4} + (x+4) + (x-4) = 400$$

$$6\frac{1}{4}x = 400$$

$$\frac{25}{4}x = 400$$

$$x = 64$$

$$\frac{16}{400} \cdot \frac{4}{25}$$

$$256 + 16 + 68 + 60$$

$$272 + 128$$

$$400$$