Solving Systems of Equations by Graphing

## EXAMPLE

Solve the system by graphing: $\left\{\begin{array}{l}y=-\frac{1}{3} x+7 \\ -2 x+4 y=8\end{array}\right.$
Step 1: Graph the first equation. Start at ( 0,7 ), then go down 1 and right 3. Continue the pattern.

Step 2: Graph the second equation. One strategy is to get $y$ by itself and use slope-intercept rules. If you add 2 x to both sides, you get $4 y=8+2 x$. Then if you divide everything by 4 , you get $y=2+\frac{1}{2} x$. Another strategy is to make a table and find some $(x, y)$ pairs that make the equation true. Three easy points that would make $-2 x+4 y=8$ true are ( 0,2 ), ( $-4,0$ ), and ( $-2,1$ ).


Solution: $(6,5)$

Step 3: Connect the points. You will see that the slope of the second line is $1 / 2$. Continue this pattern until both lines intersect. The intersection point is $(6,5)$.

Solve each system by graphing both equations and finding the point of intersection.

1) $\left\{\begin{array}{c}y=\frac{1}{2} x+2 \\ y=-\frac{2}{3} x+9\end{array}\right.$
2) $\left\{\begin{array}{c}y=2 x-8 \\ y=-3 x+7\end{array}\right.$
3) $\left\{\begin{array}{c}y=x+5 \\ y=4 x-7\end{array}\right.$



4) $\left\{\begin{array}{c}y=\frac{1}{2} x+8 \\ y=-\frac{1}{3} x+3\end{array}\right.$
5) $\left\{\begin{array}{l}y=\frac{1}{4} x+3 \\ y=-x-2\end{array}\right.$
6) $\left\{\begin{array}{c}y=-\frac{5}{2} x \\ y=-4 x+6\end{array}\right.$



7) Choose one of the systems from \#1-6 and check your solution by plugging both numbers into both equations.
8) Which of the possibilities could be point $\mathbf{M}$ ? Which could be point $\mathbf{N}$ ?
A. $(9,1)$
B. $(5,2)$
C. $(6,4)$
D. $(7,3)$

b) Graph both equations. Hint: you will need to scale your yaxis by more than 1 .
c) Write the point of intersection, and explain what both of these numbers mean in the context of the problem.
9) $\left\{\begin{array}{c}y=3 x-2 \\ y=-\frac{2}{3} x-2\end{array}\right.$


| $\begin{array}{c}\text { (For help on how to graph } \\ \text { the "standard form" }\end{array}$ |
| :---: |

13) $\left\{\begin{array}{c}x+y=8 \\ y=\frac{3}{2} x-7\end{array}\right.$
equations, look at "step
$2^{\prime \prime}$ in the example on the
front or the back side of your guided notes!)
 with no additional charges.
a) Write an equation for each situation where $\mathbf{x}$ is the number of hours and $\mathbf{y}$ is the total cost. axis by more than 1 .
14) Creative Crafts gives scrapbooking lessons for $\$ 15$ per hour plus a $\$ 20$ supply charge. Scrapbooks Incorporated gives lessons for $\$ 20$ per hour

15) $\left\{\begin{array}{l}y=\frac{2}{3} x+4 \\ y=\frac{2}{3} x+1\end{array}\right.$

16) $\left\{\begin{array}{c}5 x+3 y=30 \\ 10 x-2 y=20\end{array}\right.$

